

# Core Collapse Supernovae and EOS thermal effects

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Evan O'Connor  
NP3M Seminar  
September 7, 2023

**NAISS**

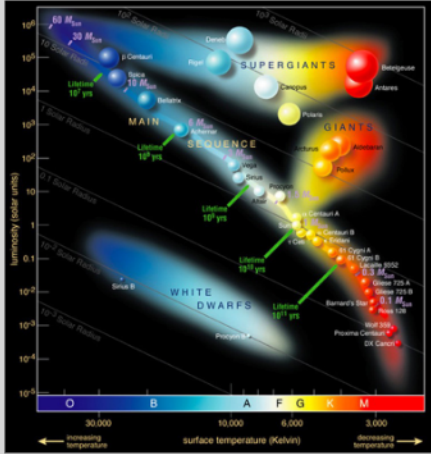
  
Swedish  
Research Council

  
Oskar Klein  
centre

  
Stockholms  
universitet

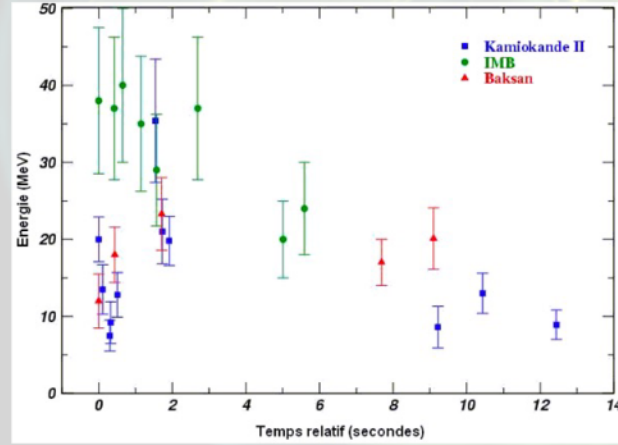
# Supernovae have a broad connection to the Universe

## Stellar Evolution

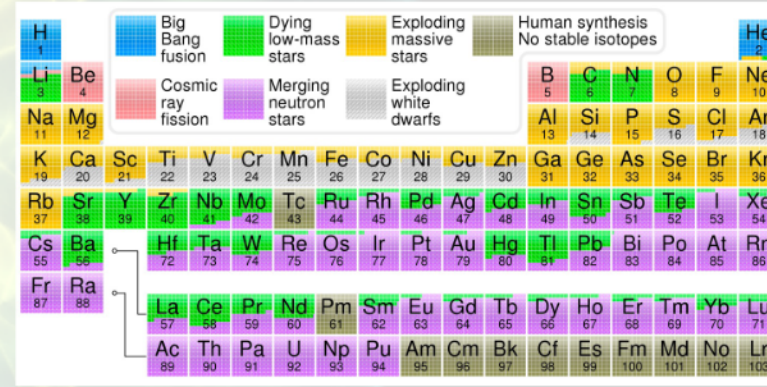


ESO

## Neutrinos & Gravitational Waves

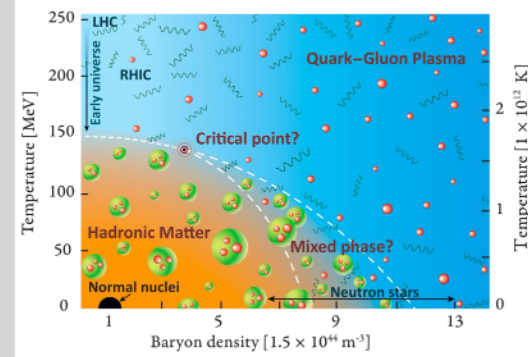


## Nucleosynthesis



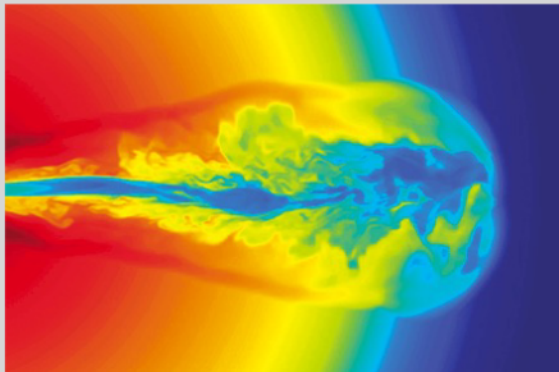
Wikimedia/Jennifer Johnson

## Extreme Physics



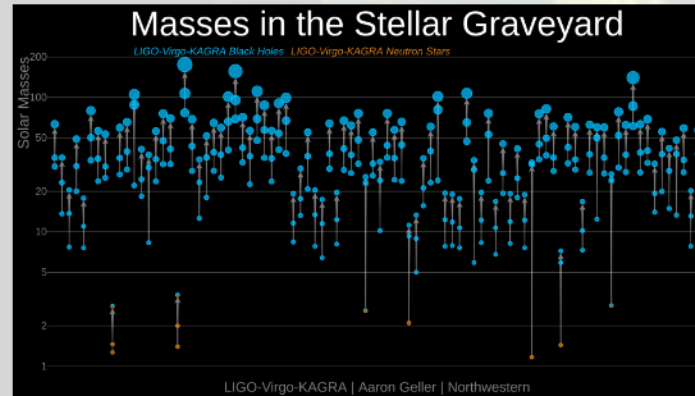
Contemporary Physics Education Project (CPEP)

## Long gamma-ray burst



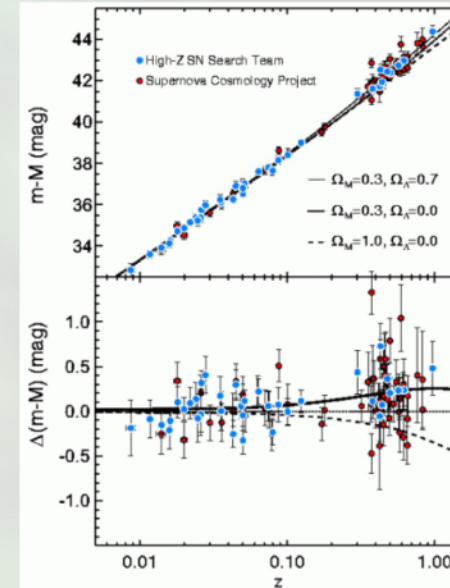
Science/MacFadyen

## Neutron Stars & Black Holes



LIGO/VIRGO

## Cosmology



High-Z & SCP

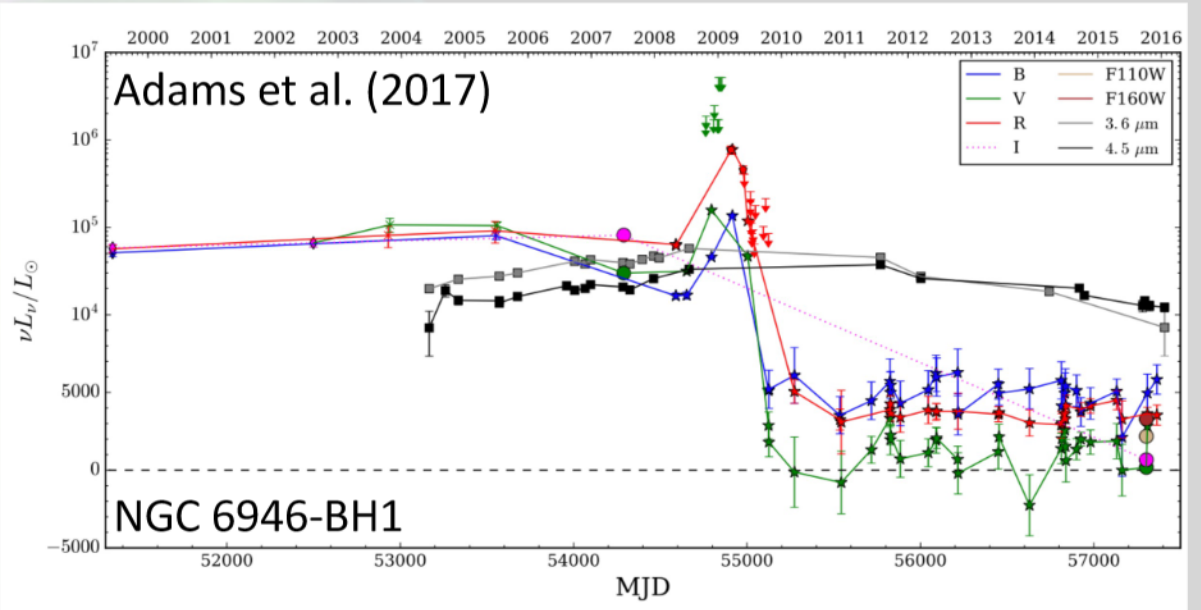
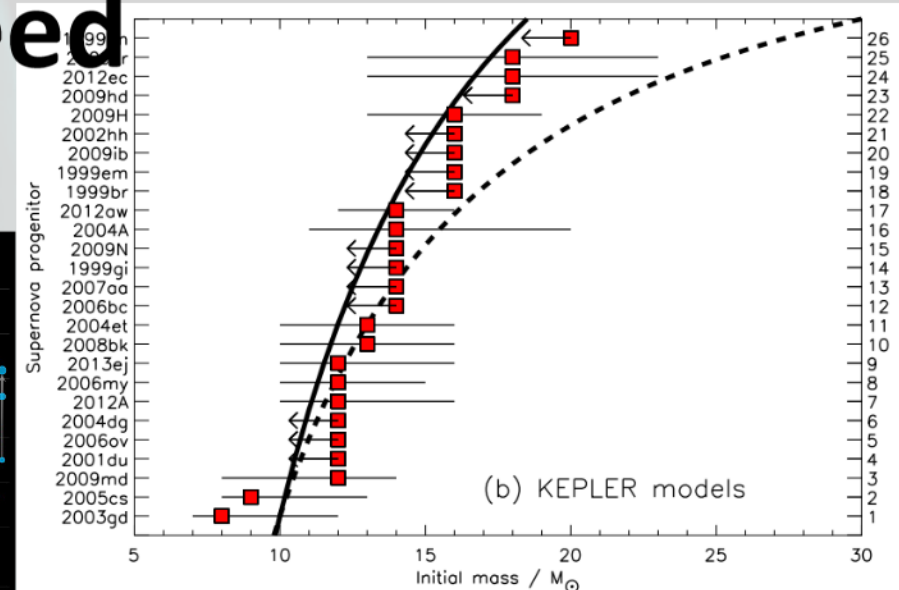
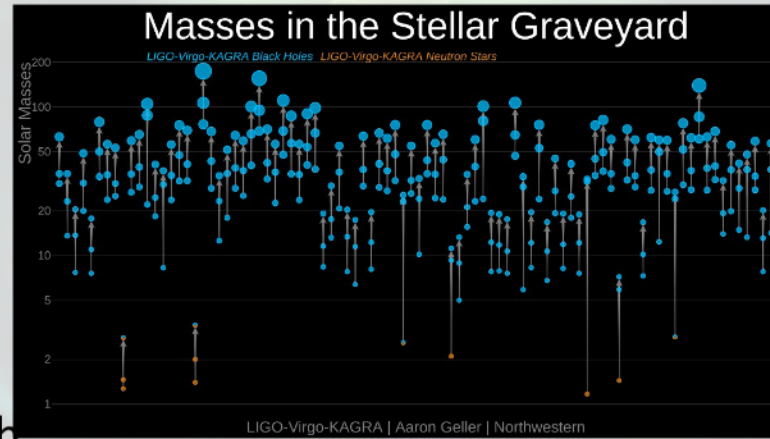
## Galaxy Evolution



Hubble

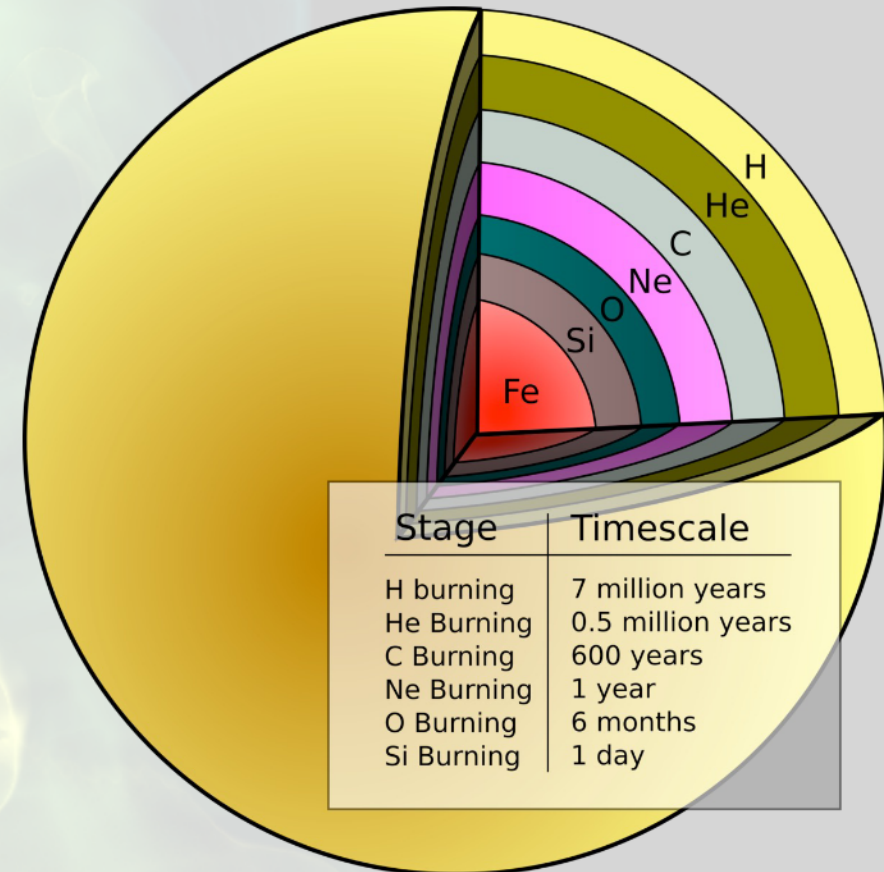
# Not all core collapses will succeed

- Progenitors of Type II-P CCSNe suggest a maximum mass of  $\sim 16.5 \pm 1.5 M_{\text{sun}}$  – but RSG extend to  $25 M_{\text{sun}}$  (Smartt 2015)
- Black holes exist! We see stellar mass black holes in binaries with stars and with other black holes
- We have seen preliminary evidence that massive stars disappear, perhaps following a failed supernovae



# Stellar Collapse: Building the Core

- Stars spend most of their lives burning hydrogen.
- The product – Helium – settles in the core and will burn when temperatures increase sufficiently.
- For massive stars ( $M > 8-10M_{\text{sun}}$ ), the process continues through Carbon, Oxygen, ... , up to Iron.
- This process does not continue past iron as iron is one of the most tightly bound nuclei.
- Iron core builds up in center of star.

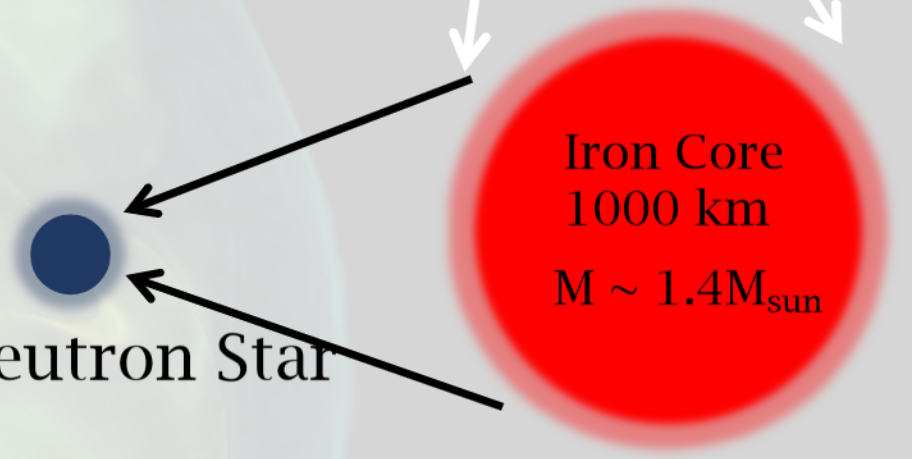
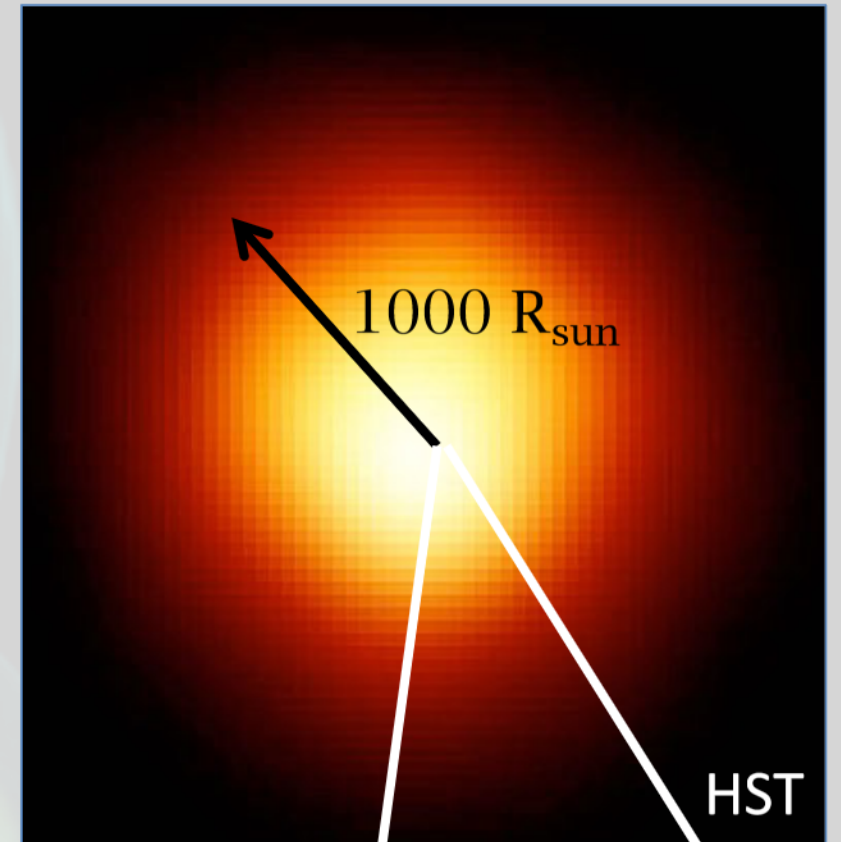


A. C. Phillips, *The Physics of Stars*, 2nd Edition (Wiley, 1999).

# Collapse Phase

- Most massive stars core collapse during the red supergiant phase
- CCSNe are triggered by the collapse of the iron core (~1000km, or  $1/10^6$  of the star's radius)
- Collapse ensues because electron degeneracy pressure can no longer support the core against gravity

$$-\frac{3}{5} \left[ \frac{GM^2}{1000\text{km}} - \frac{GM^2}{12\text{km}} \right] \sim 300 \times 10^{51} \text{ ergs}$$

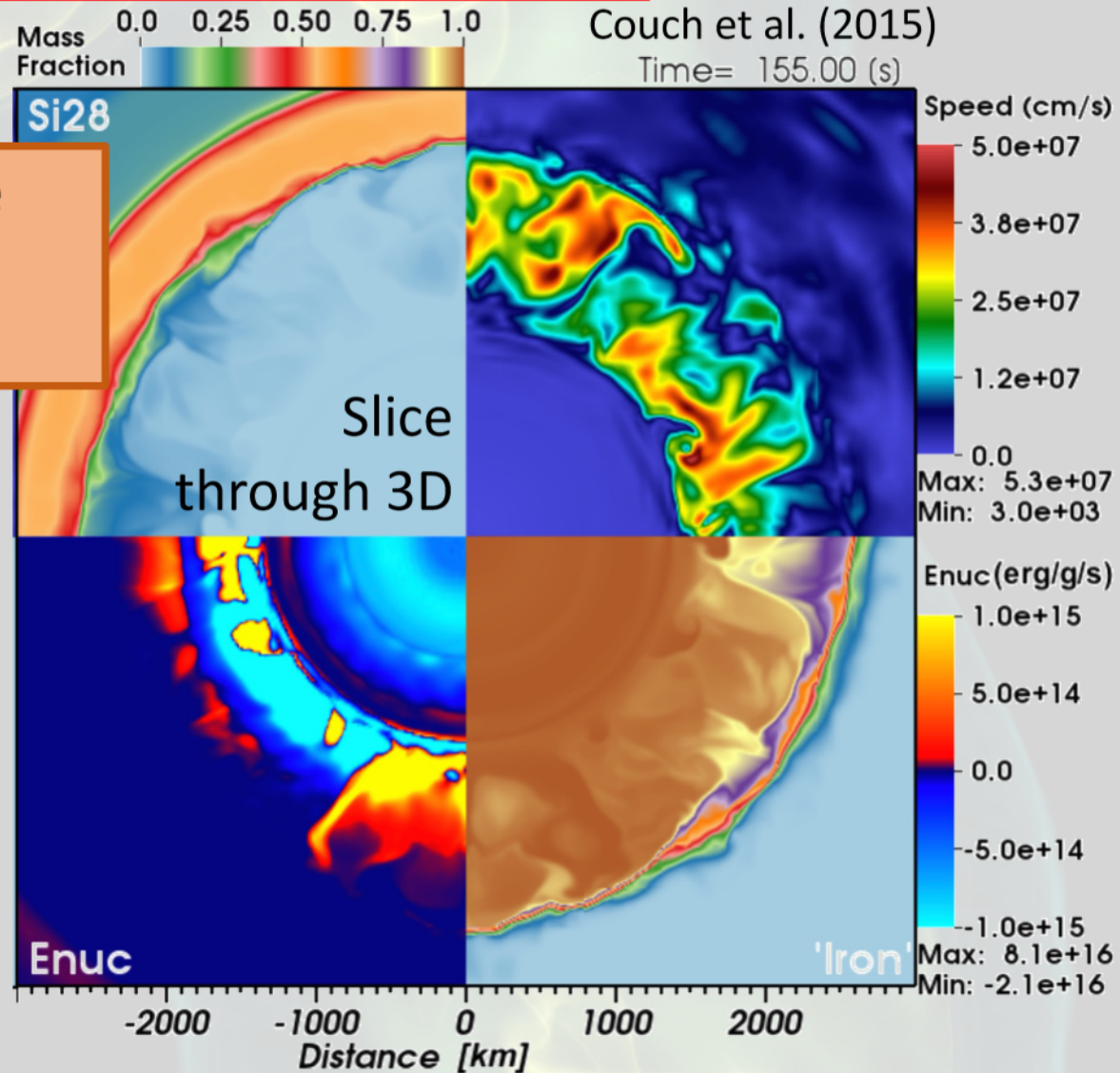


# Not a pristine onion...

Couch et al. (2015)

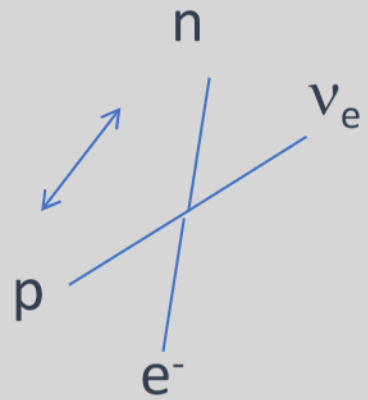
Time= 155.00 (s)

Final burning stages are violent, *not* spherically symmetric.



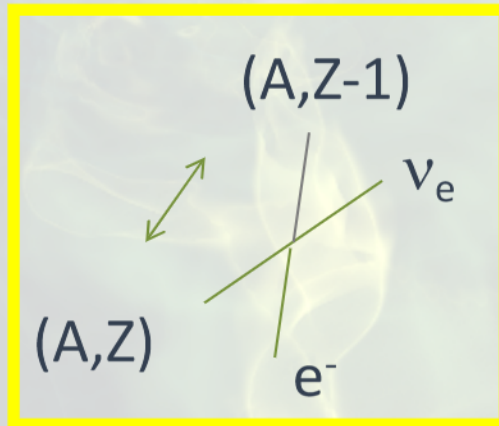
# Collapse Phase: Role of Neutrinos

- Emission of neutrinos deleptonizes the core and accelerates collapse
- The emission ultimately sets the final  $Y_e$  of the core

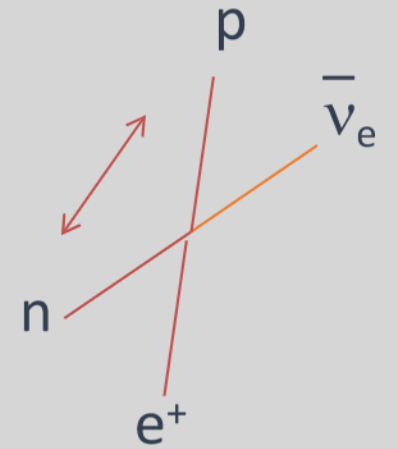


Electron capture on free protons. Cross section is very high, but suppressed because number of free protons is low

- Heavy-lepton neutrino production is highly suppressed because temperature is so low



Electron capture on heavy nuclei. Abundance is very high, cross section is somewhat suppressed because of energetic cost of converting proton to neutron in a nucleus.

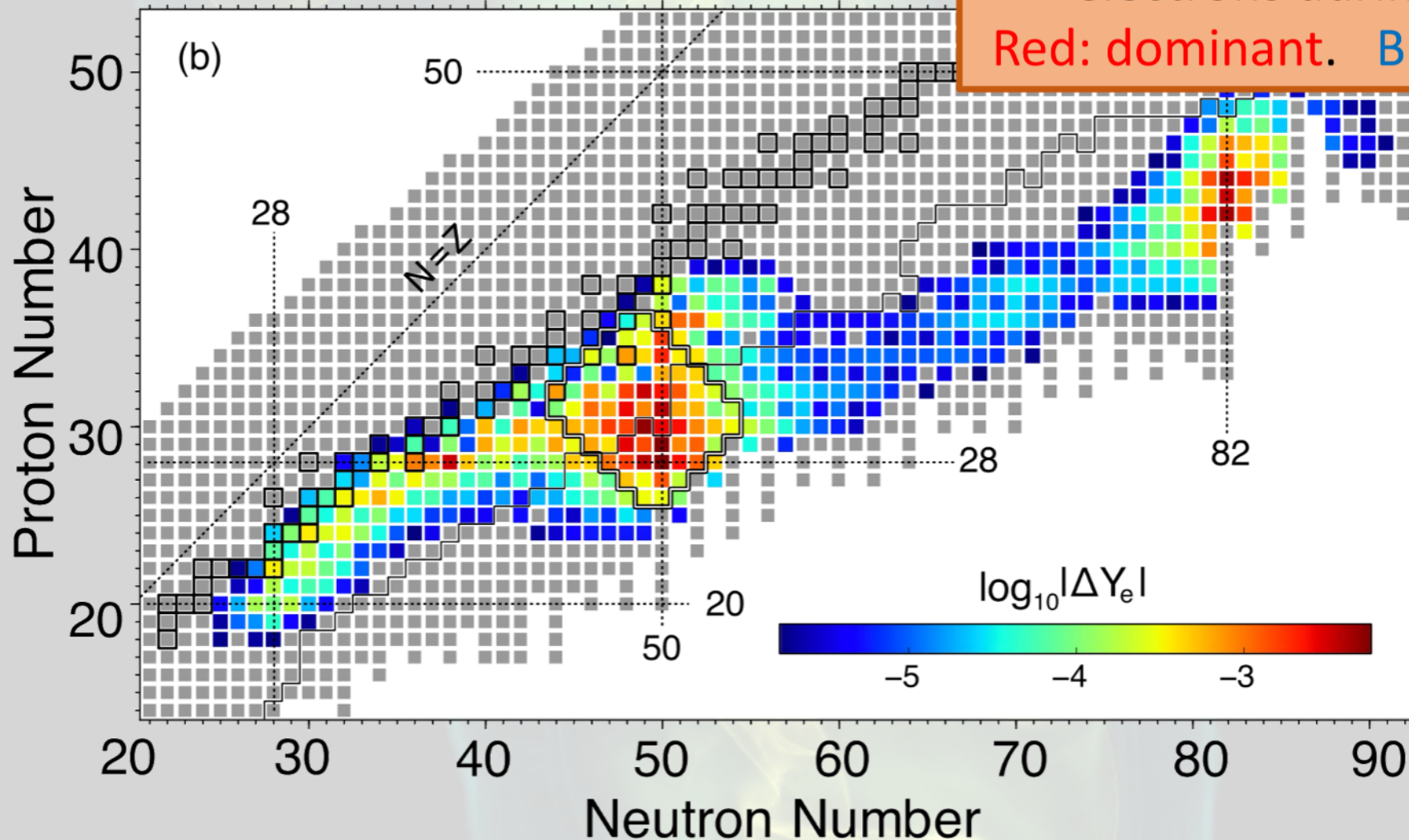


Positron capture on free neutrons. Suppressed because positron density is very low due to high electron chemical potential

# Electron Captures during Collapse

Sullivan et al. (2016), Titus et al. (2018)

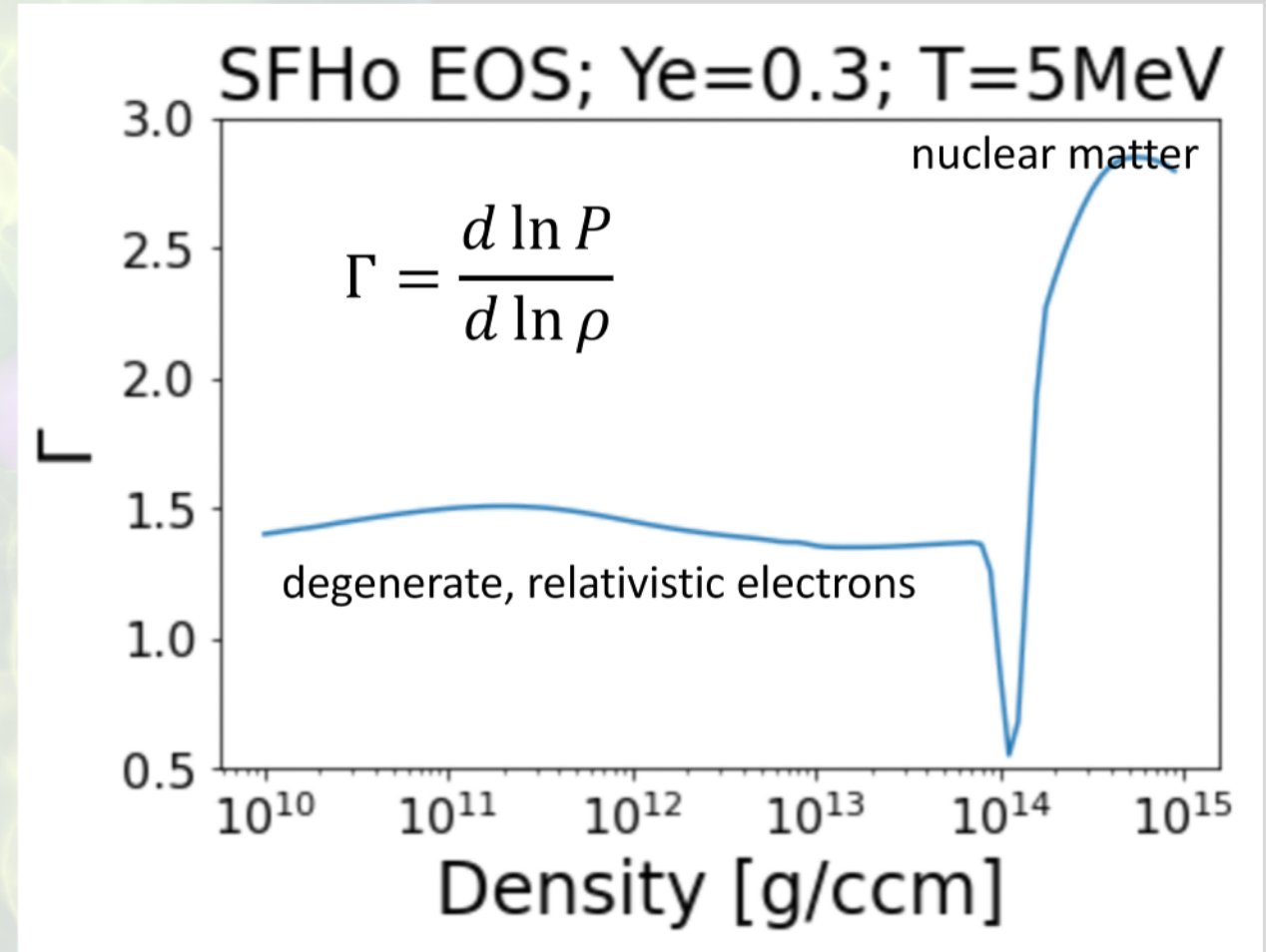
Color: contribution to capturing electrons during collapse  
Red: dominant. Blue: negligible



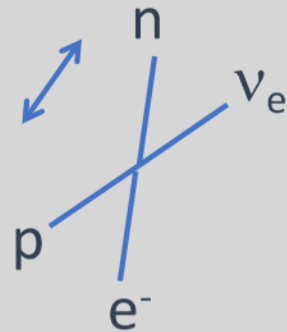


# Neutronization Burst

- When the matter reaches nuclear density the “stiffening” of the EOS halts the collapse
- The core elastically rebounds and drives a shock into the infalling matter

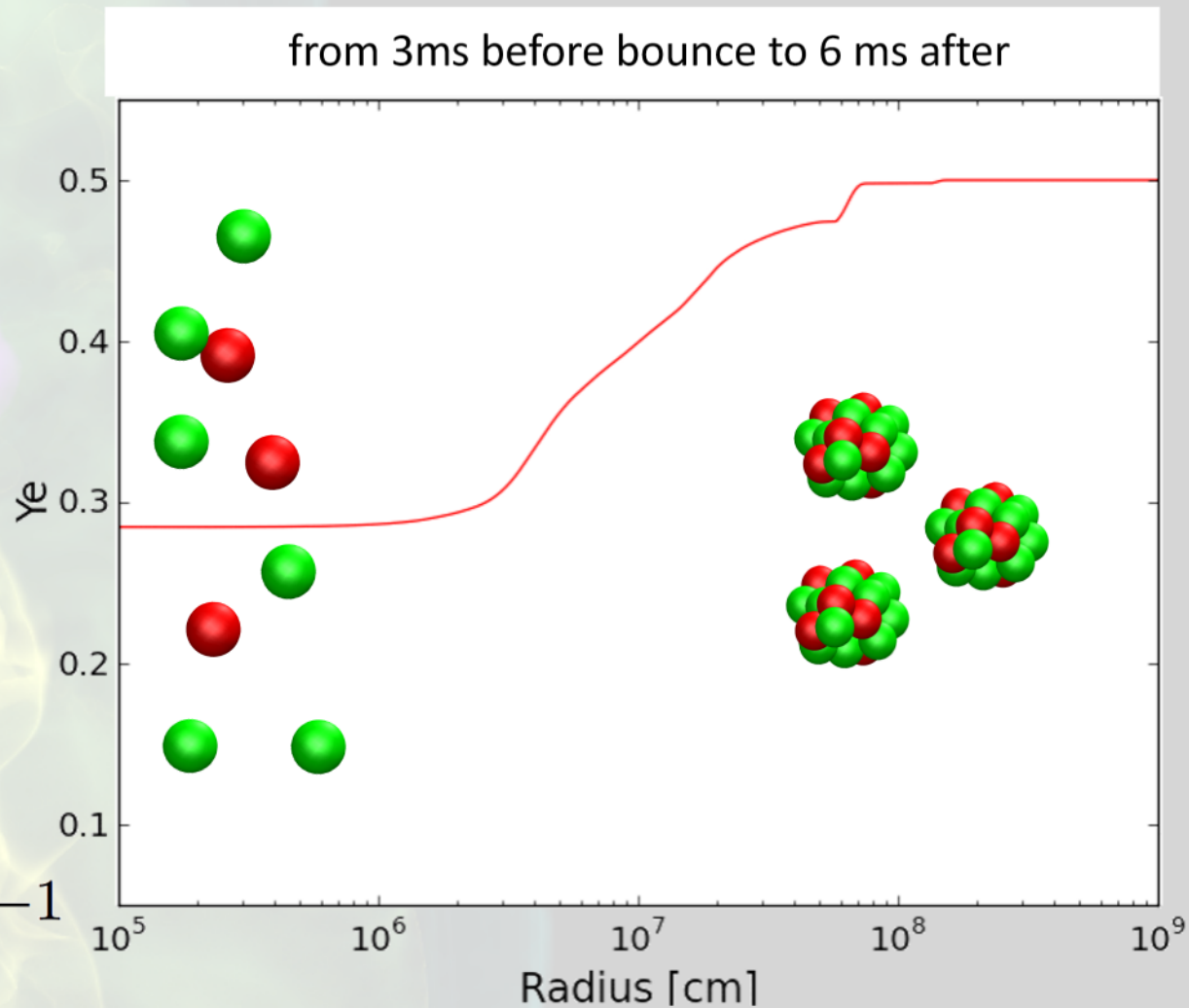


# Neutronization Burst

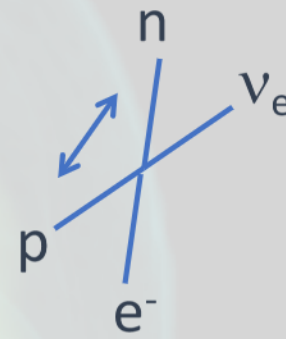


- Recently freed and no longer suppressed, protons now rapidly capture electrons, producing a burst of  $\nu_e$
- This neutronization burst is universal across core-collapse progenitors

$$\frac{1}{2} \frac{M_{\odot}}{m_N} \times 0.2 \times \frac{10 \text{ MeV}}{5 \text{ ms}} \sim 4 \times 10^{53} \text{ erg s}^{-1}$$

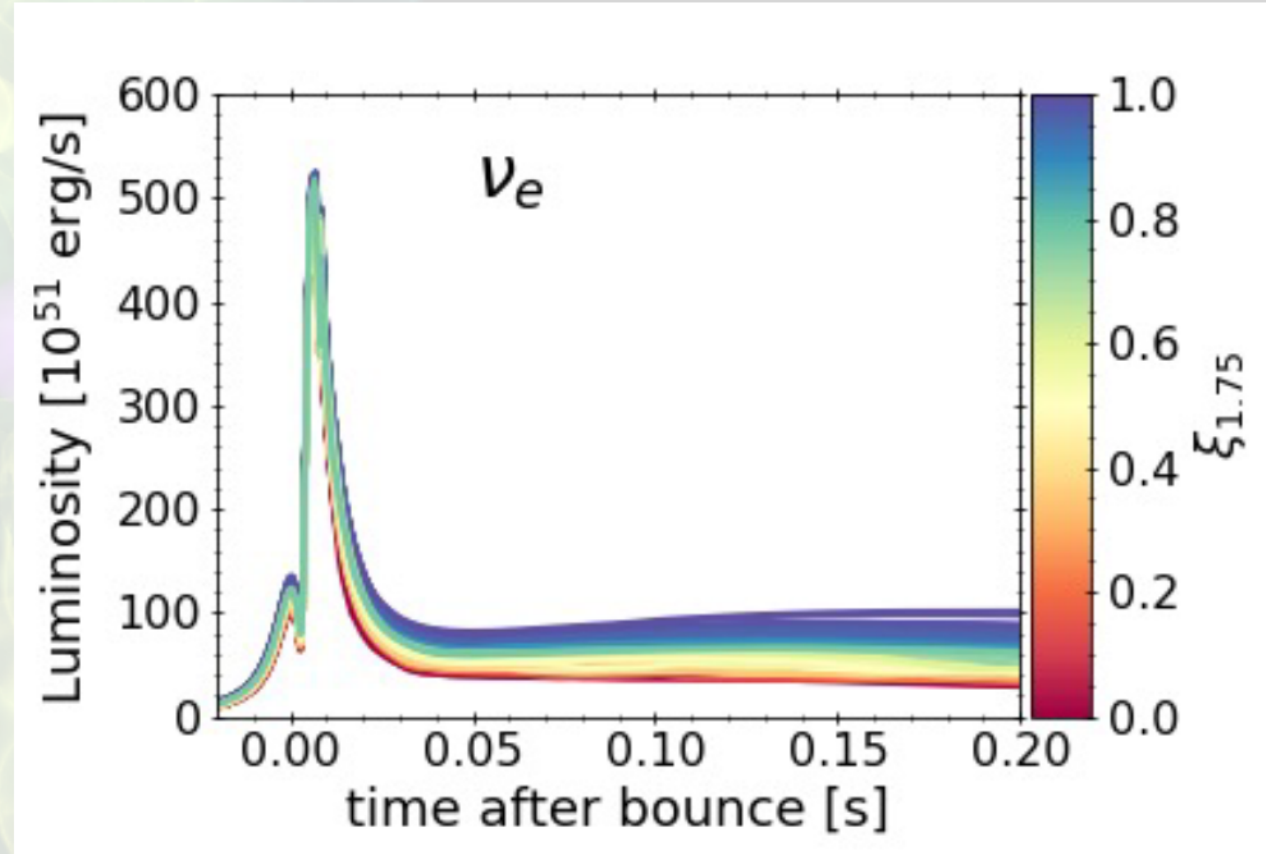


# Neutronization Burst



FLASH simulations, 149 progenitors, SFHo EOS, Segerlund et al. (2021)

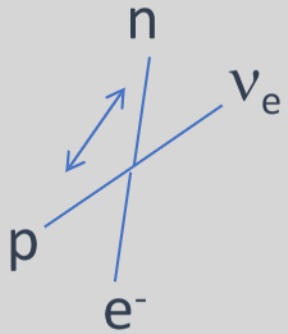
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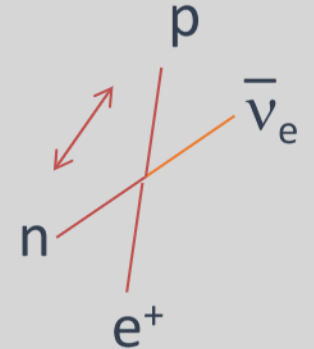
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# Accretion Phase: Role of Neutrinos

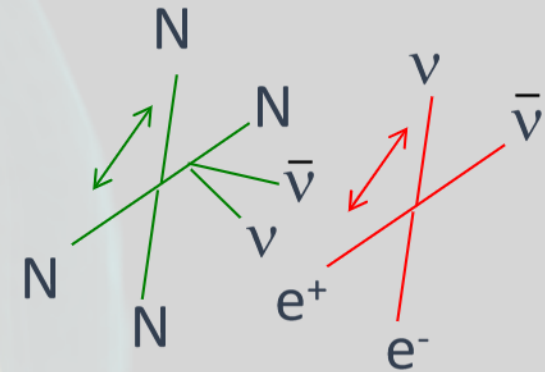
- After the burst,  $\nu_e$  and anti- $\nu_e$  emission is powered by accretion
- Infalling matter is shock heated and then is cooled via neutrino emission



- Charged current processes dominant production
- Thermal production processes dominate at high densities where neutrinos are trapped for seconds

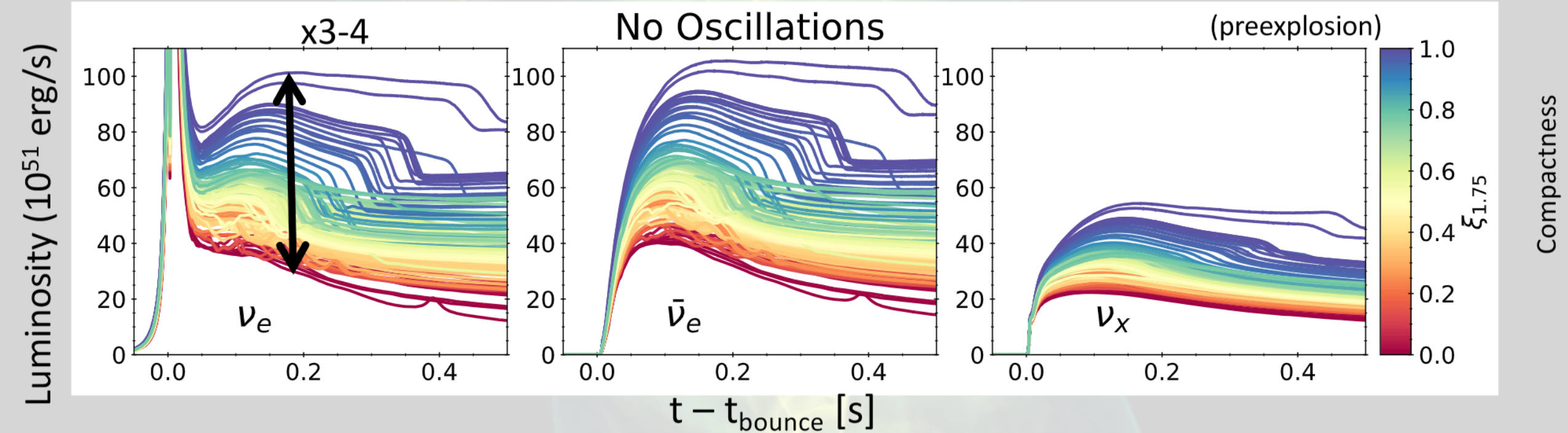


- Thermal emission is dominant production process for heavy lepton neutrinos as  $T$  is too low for charged-current processes with  $\mu$ 's and  $\tau$ 's



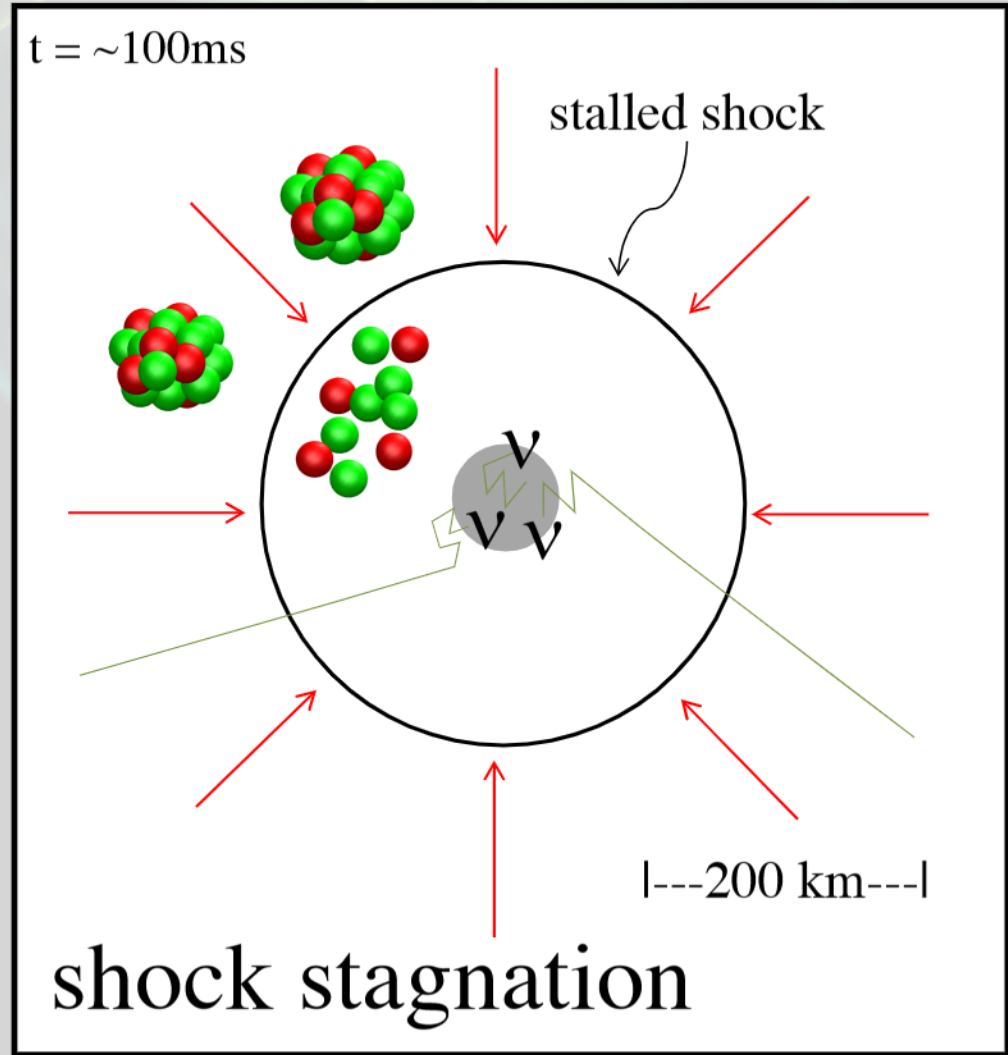
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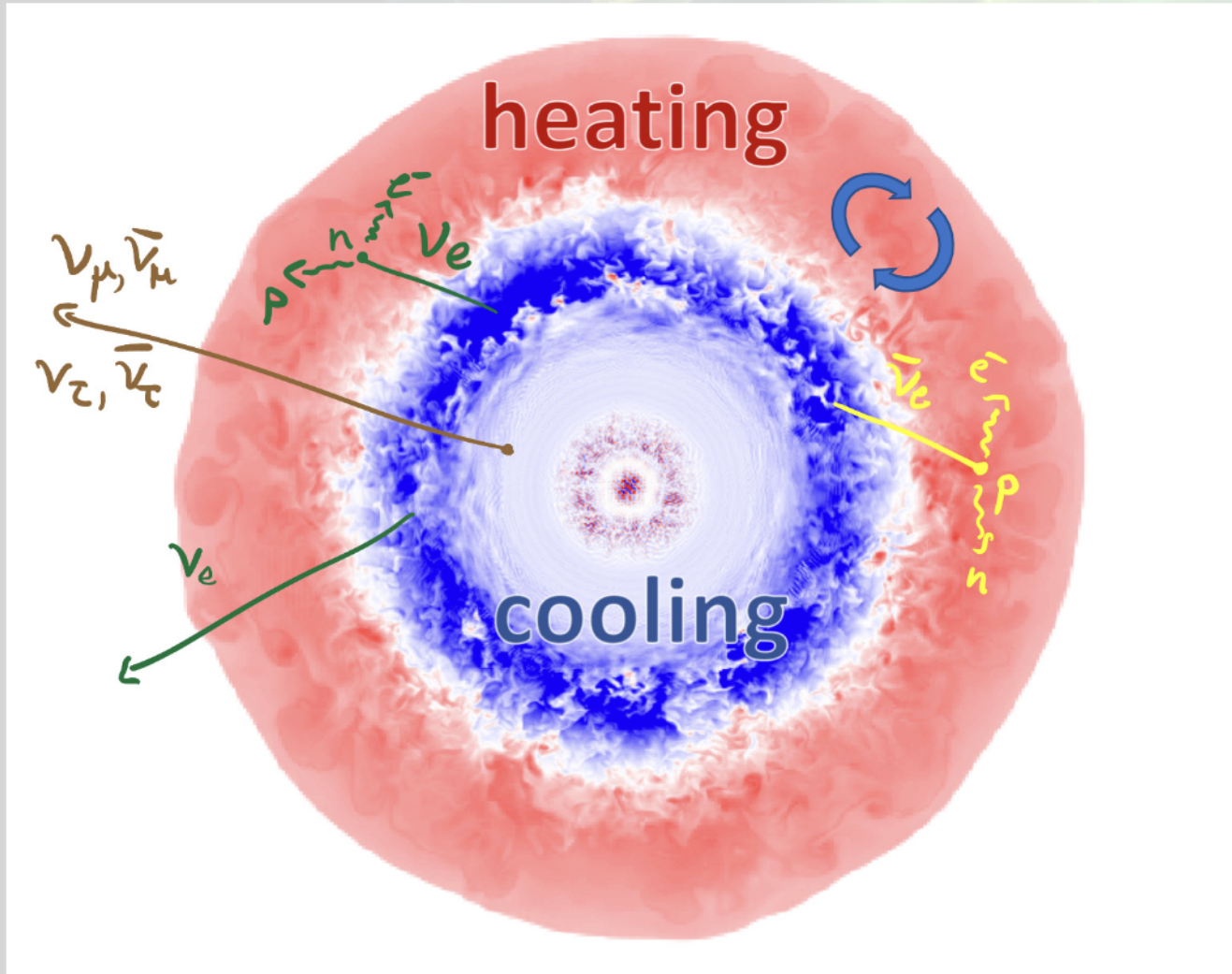


Learn about progenitor structure  
from neutrino observation of a  
galactic supernova

# CCSNe: The Explosion?



# The Core-Collapse Supernova Problem

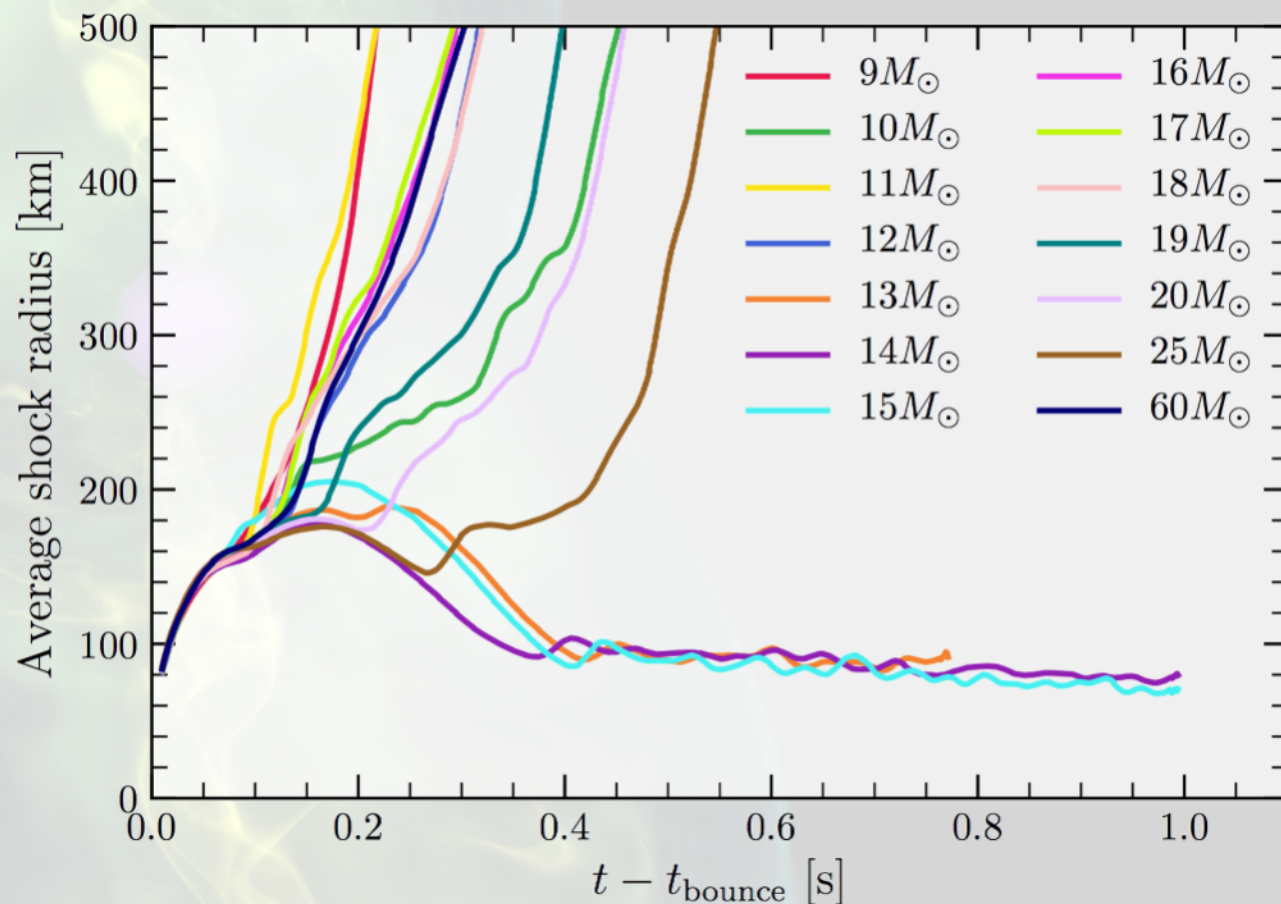


- The naive `prompt` mechanism fails
- The prevailing mechanism is the **turbulence-aided neutrino mechanism**
  - Neutrinos from core heat outer layers
  - Drives convection
  - Turbulence pressure support aids heating and drive explosion
- Very successful in 2D, also successful in 3D.

# Successful CCSN explosions

Burrows et al. (2019)

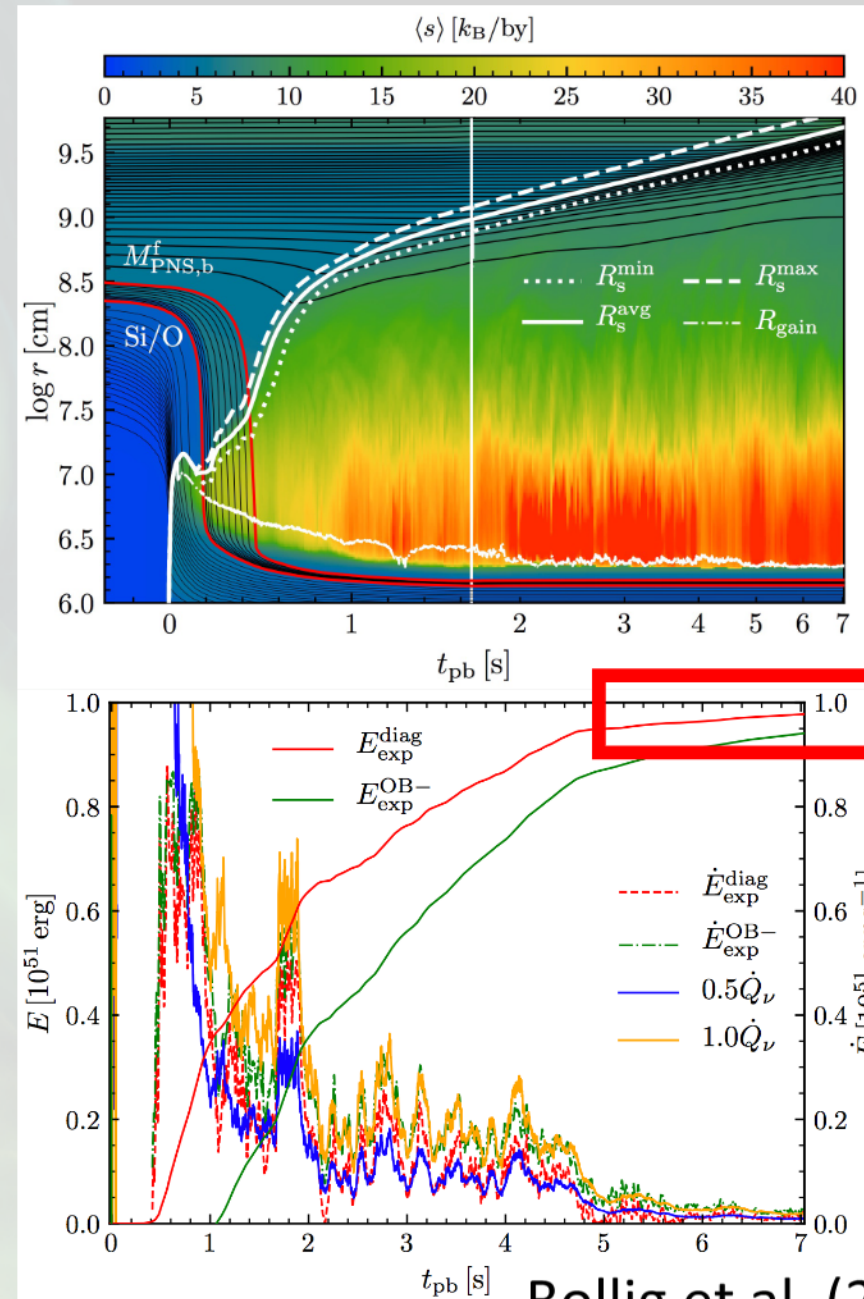
- Routinely, modern, state-of-the-art, symmetry-free, simulation codes obtain explosions across the progenitor spaces
- Suggest that canonical observed energies (0.5-1 Bethe) are achievable in the turbulence-aided neutrino mechanism, if you wait long enough





# Successful CCSN explosions

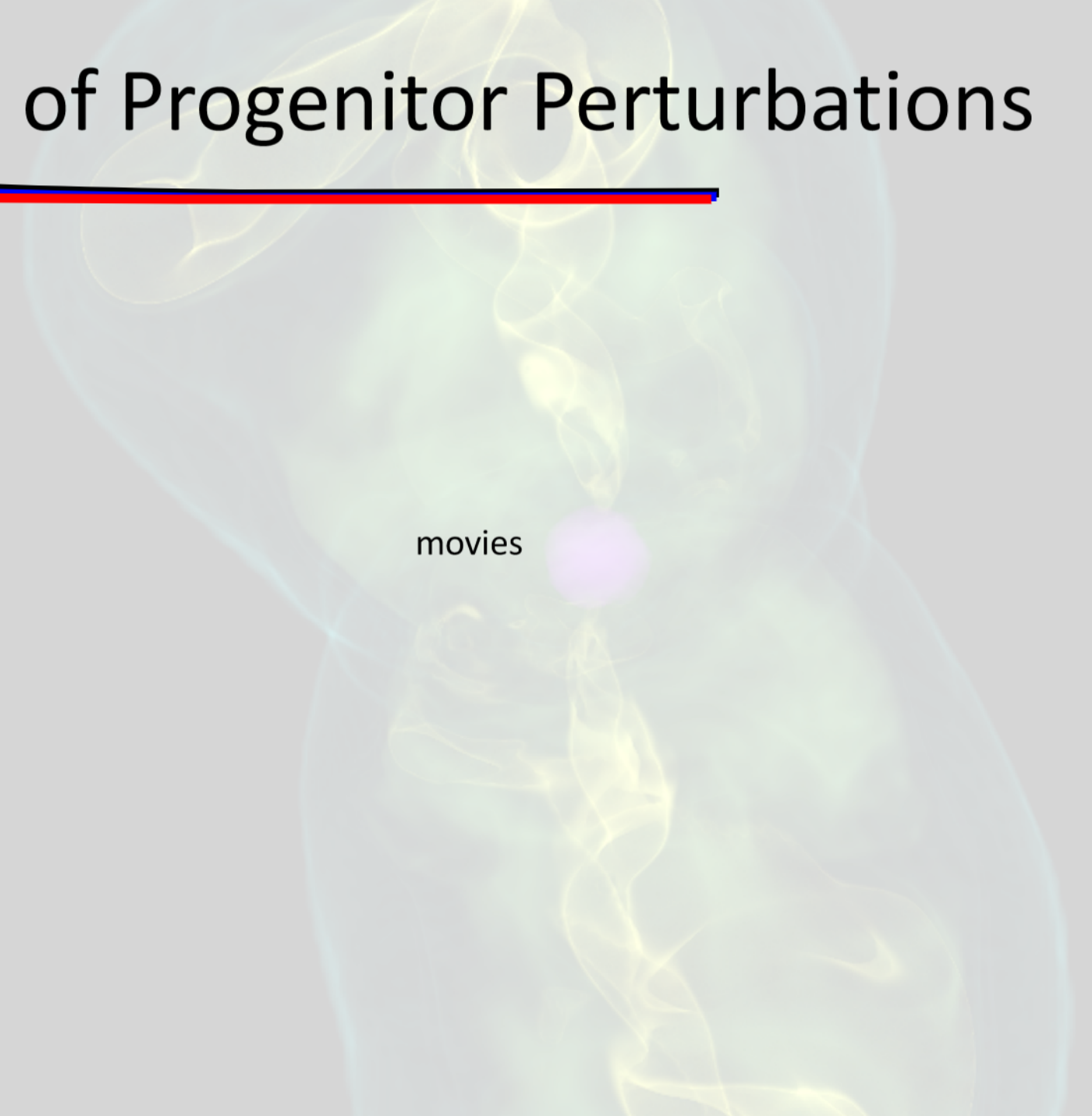
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# Impact of Progenitor Perturbations



movies



# Core Collapse Supernovae and **EOS thermal effects**

Evan O'Connor  
NP3M Seminar  
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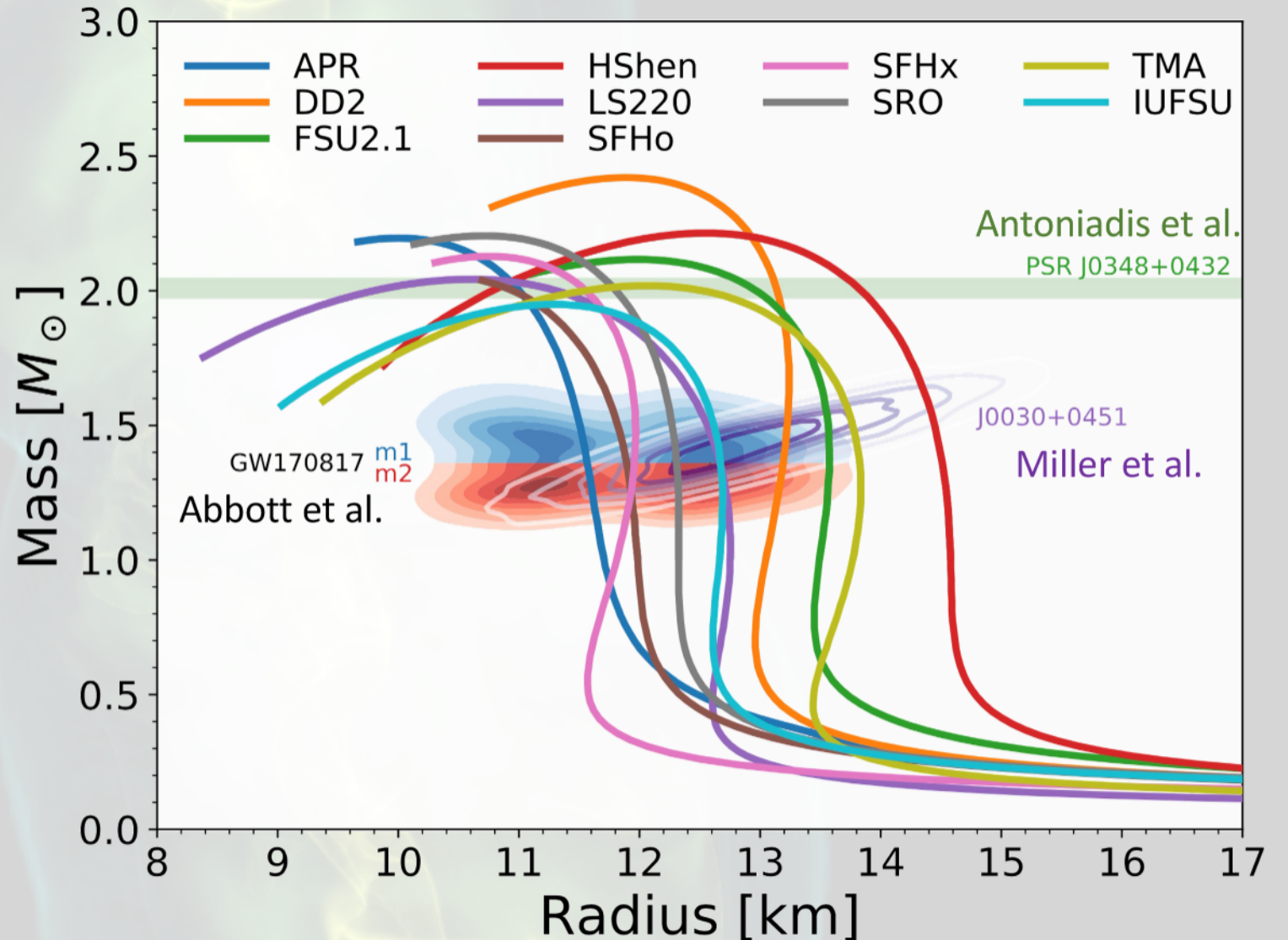


# Nuclear Equation of State and Core Collapse

Wide variety of finite temperature EOS to choose from

Need:

- $1e-12 < n_b [\text{fm}^{-3}] < 10$
- $0.01 < T [\text{MeV}] < 150$
- $0 < Y_p < 0.6$

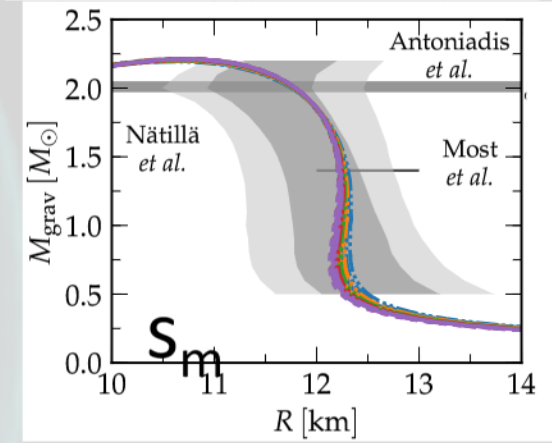
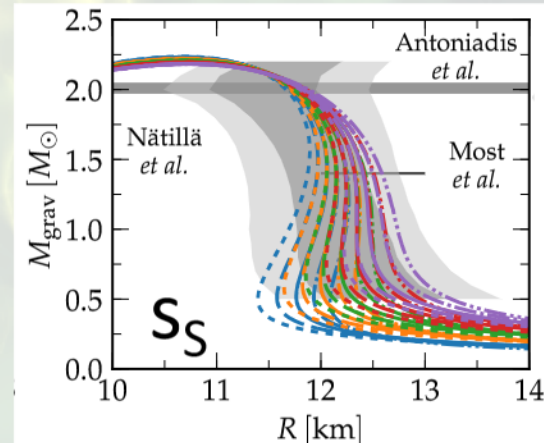
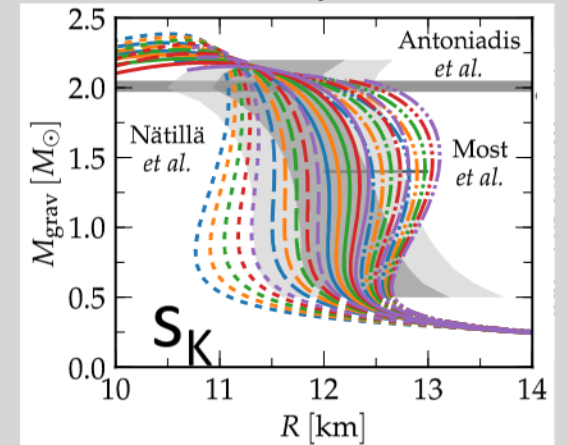
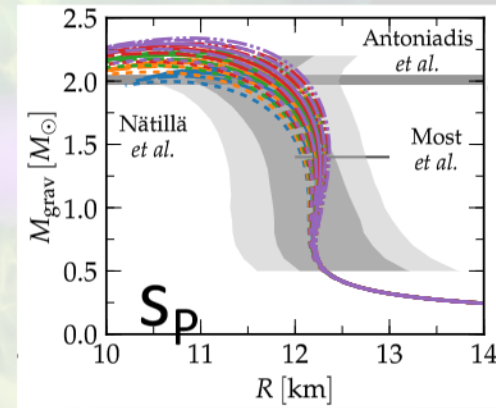


# Impact assessed only with systematic studies

da Silva Schneider et al. (2019b)

Set	Quantity	Range	This work	Units
$s_M$	$m^*$	$0.75 \pm 0.10$	$0.75 \pm 0.10$	$m_n$
	$\Delta m^*$	$0.10 \pm 0.10$	$0.10 \pm 0.10$	$m_n$
—	$n_{\text{sat}}$	$0.155 \pm 0.005$	0.155	$\text{fm}^{-3}$
	$\epsilon_{\text{sat}}$	$-15.8 \pm 0.3$	-15.8	$\text{MeV baryon}^{-1}$
$s_S$	$\epsilon_{\text{sym}}$	$32 \pm 2$	$32 \pm 2$	$\text{MeV baryon}^{-1}$
	$L_{\text{sym}}$	$60 \pm 15$	$45 \pm 7.5$	$\text{MeV baryon}^{-1}$
$s_K$	$K_{\text{sat}}$	$230 \pm 20$	$230 \pm 15$	$\text{MeV baryon}^{-1}$
	$K_{\text{sym}}$	$-100 \pm 100$	$-100 \pm 100$	$\text{MeV baryon}^{-1}$
$s_P$	$P_{\text{SNM}}^{(4)}$	$100 \pm 50$	$125 \pm 12.5$	$\text{MeV fm}^{-3}$
	$P_{\text{PNM}}^{(4)}$	$160 \pm 80$	$200 \pm 20$	$\text{MeV fm}^{-3}$

For each of the 4 sets we construct EOSs with 0, +/- 1, and +/- 2 sigma deviations of the parameters (25 for each set, 97 overall)



# What about in a supernova?

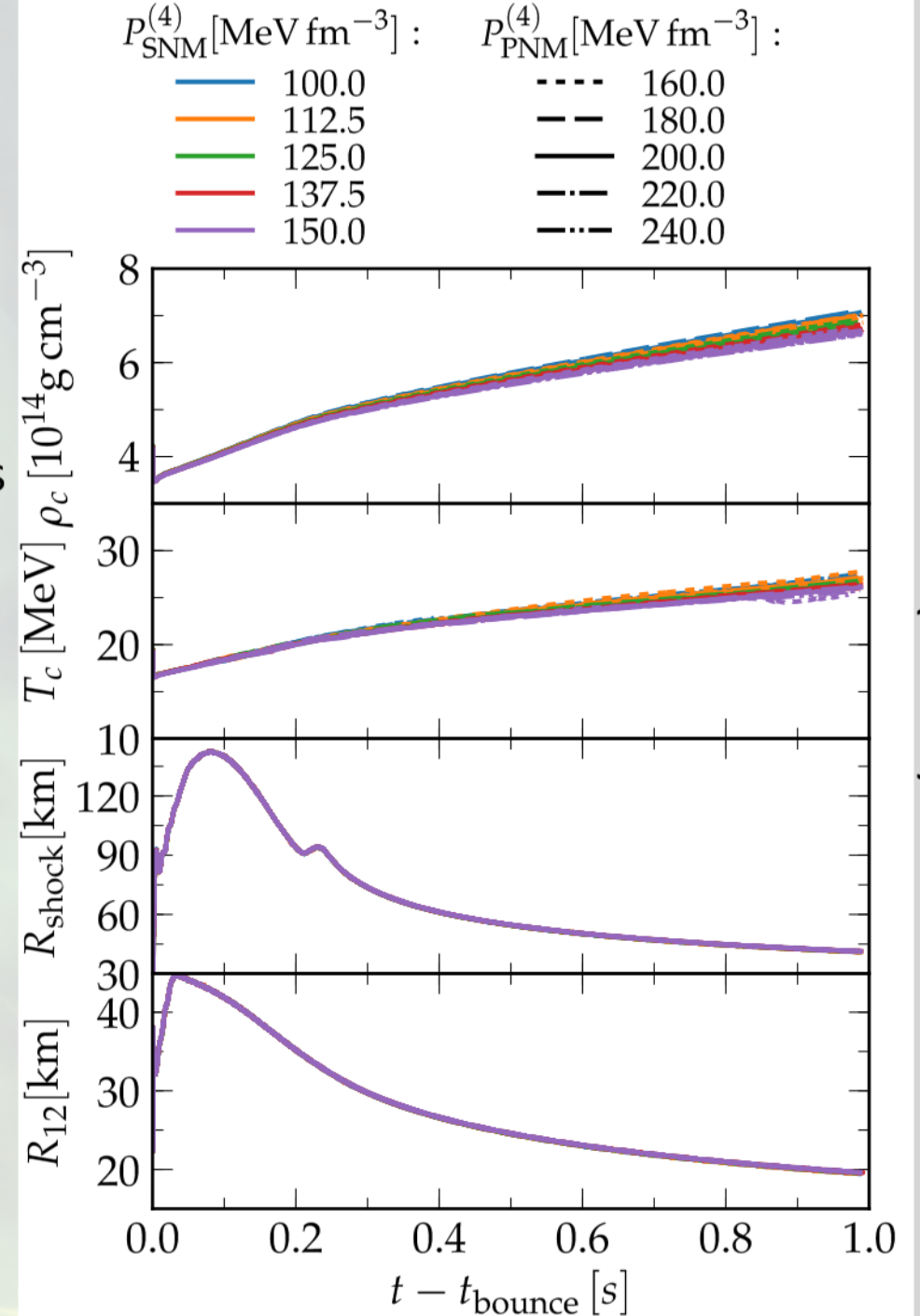
## Cold Neutron Star

- $S_p$ : Impacts maximum mass
- $S_K$ : v. large impact on NS radius
- $S_S$ : impact on low mass NS only
- $S_m$ : minimal impact

## Hot Supernova

- $S_p$ : No impact in early stages
- $S_K$ : Mild impact on radii
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**Effective mass (via the impact on the thermal EOS) plays strong and important role in supernova evolution**



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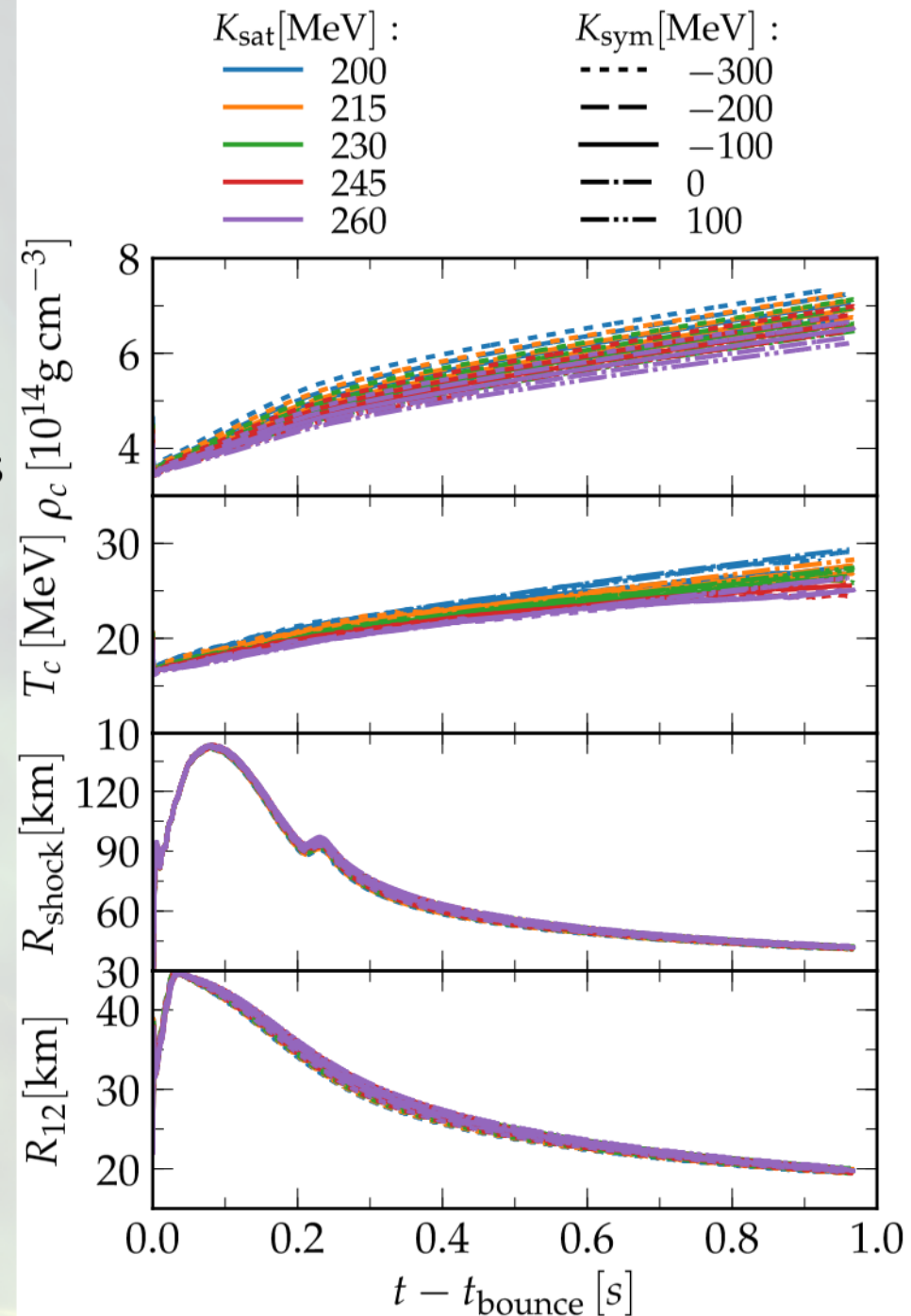
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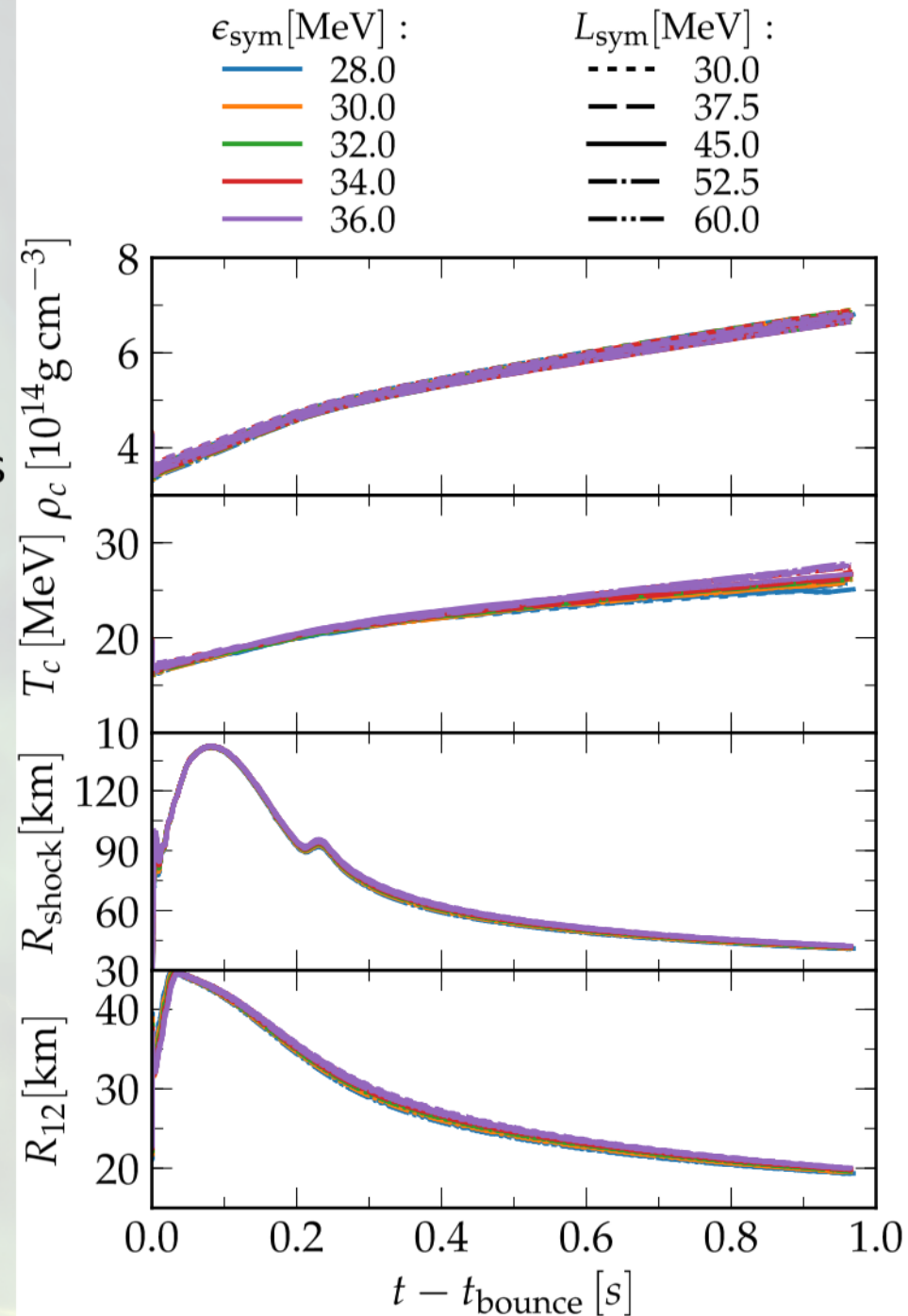
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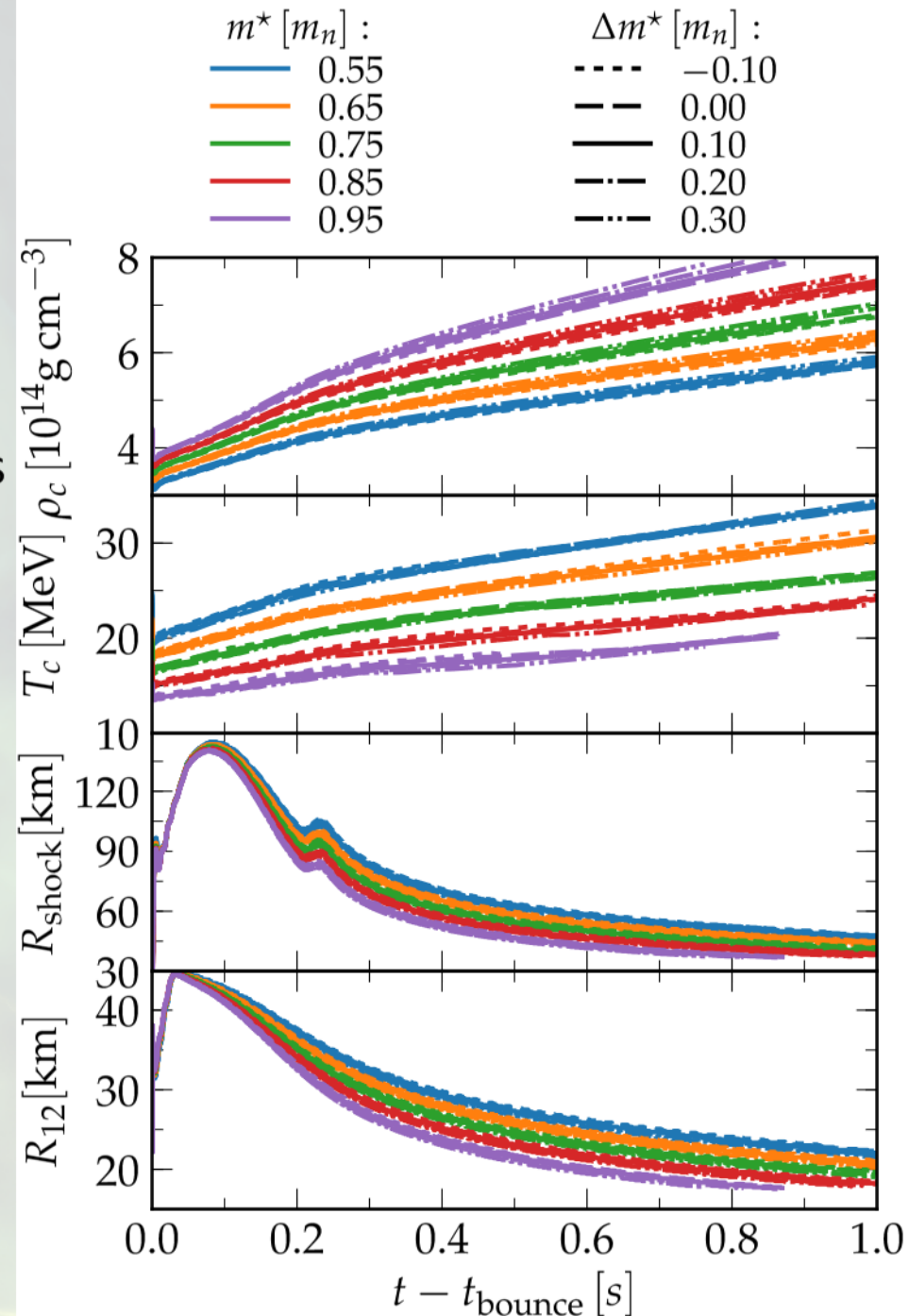
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# How does the effective mass impact the EOS?

EOS specific energy :  $\epsilon_B(n, y, T) = \epsilon_{\text{kin}}(n, y, T) + \epsilon_{\text{pot}}(n, y)$

Kinetic term (thermal term):  $\epsilon_{\text{kin}}(n, y, T) = \frac{1}{n} \left( \frac{\hbar^2 \tau_n}{2m_n^*} + \frac{\hbar^2 \tau_p}{2m_p^*} \right)$

Kinetic energy density:  $\tau_t = \frac{1}{2\pi^2} \left( \frac{2m_t^* T}{\hbar^2} \right)^{5/2} \mathcal{F}_{3/2}(\eta_t)$

Effective masses thru Skyrme terms:  $\frac{\hbar^2}{2m_t^*} = \frac{\hbar^2}{2m_t} + \alpha_1 n_t + \alpha_2 n_{-t}$

# What about in a supernova?

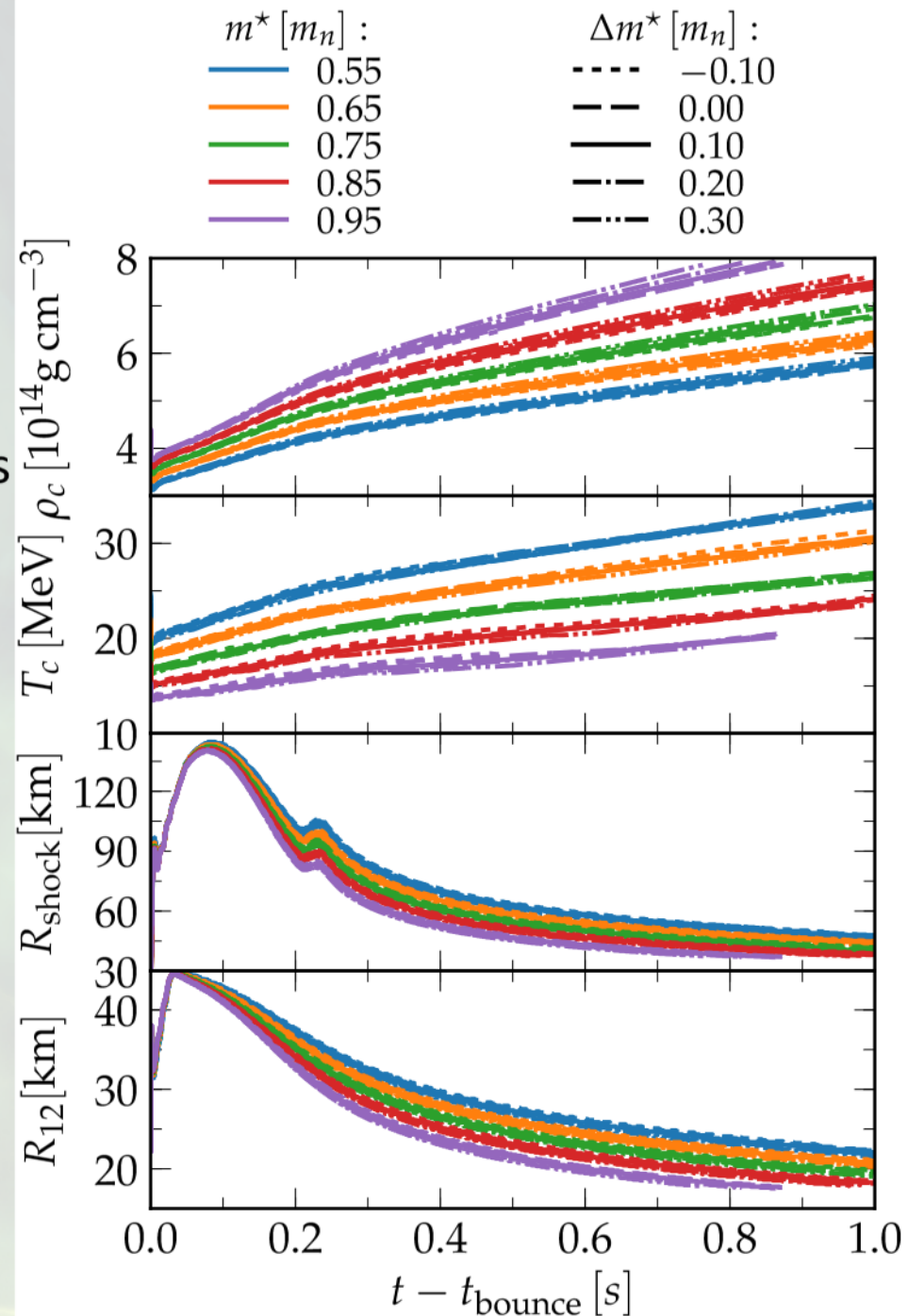
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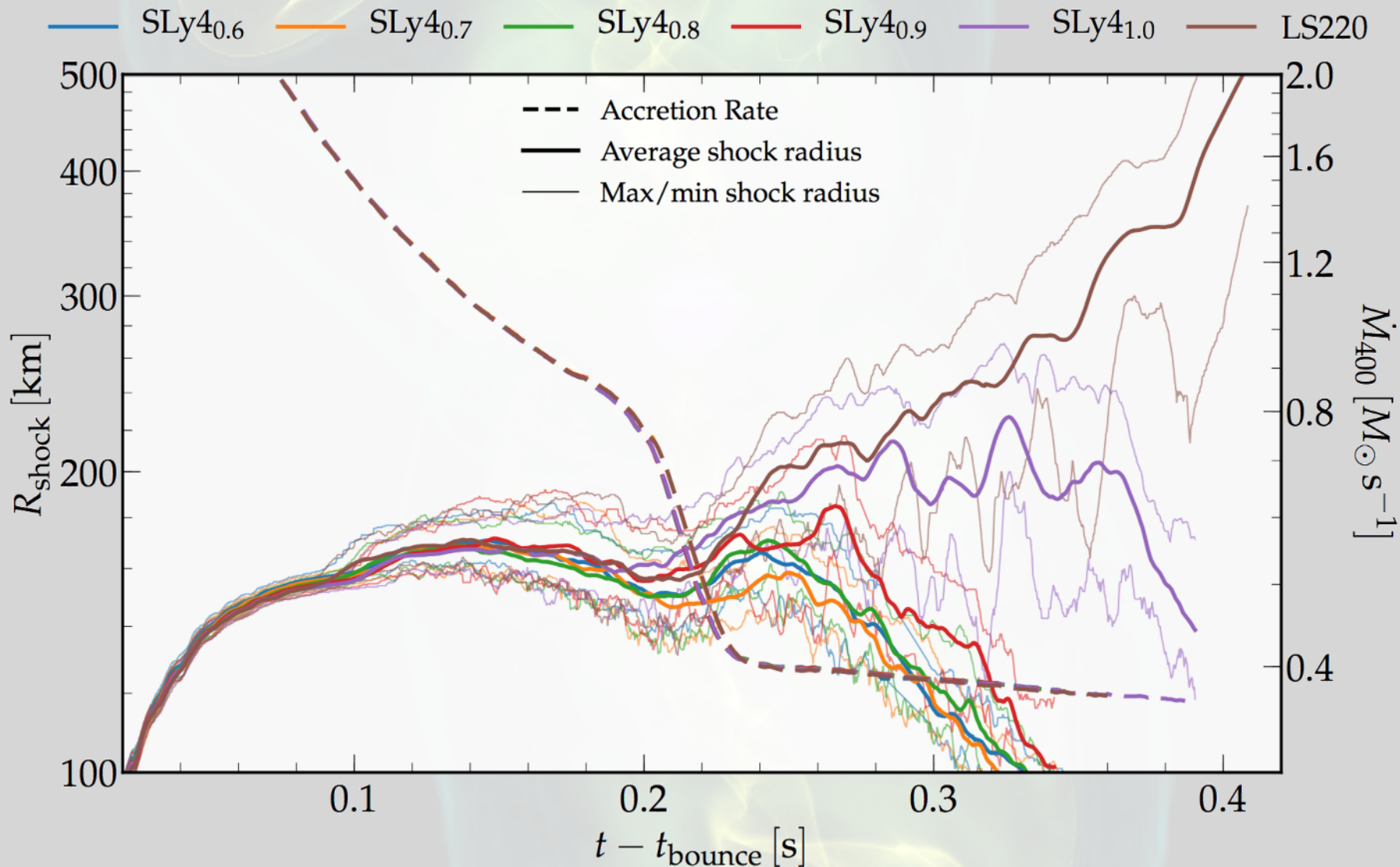
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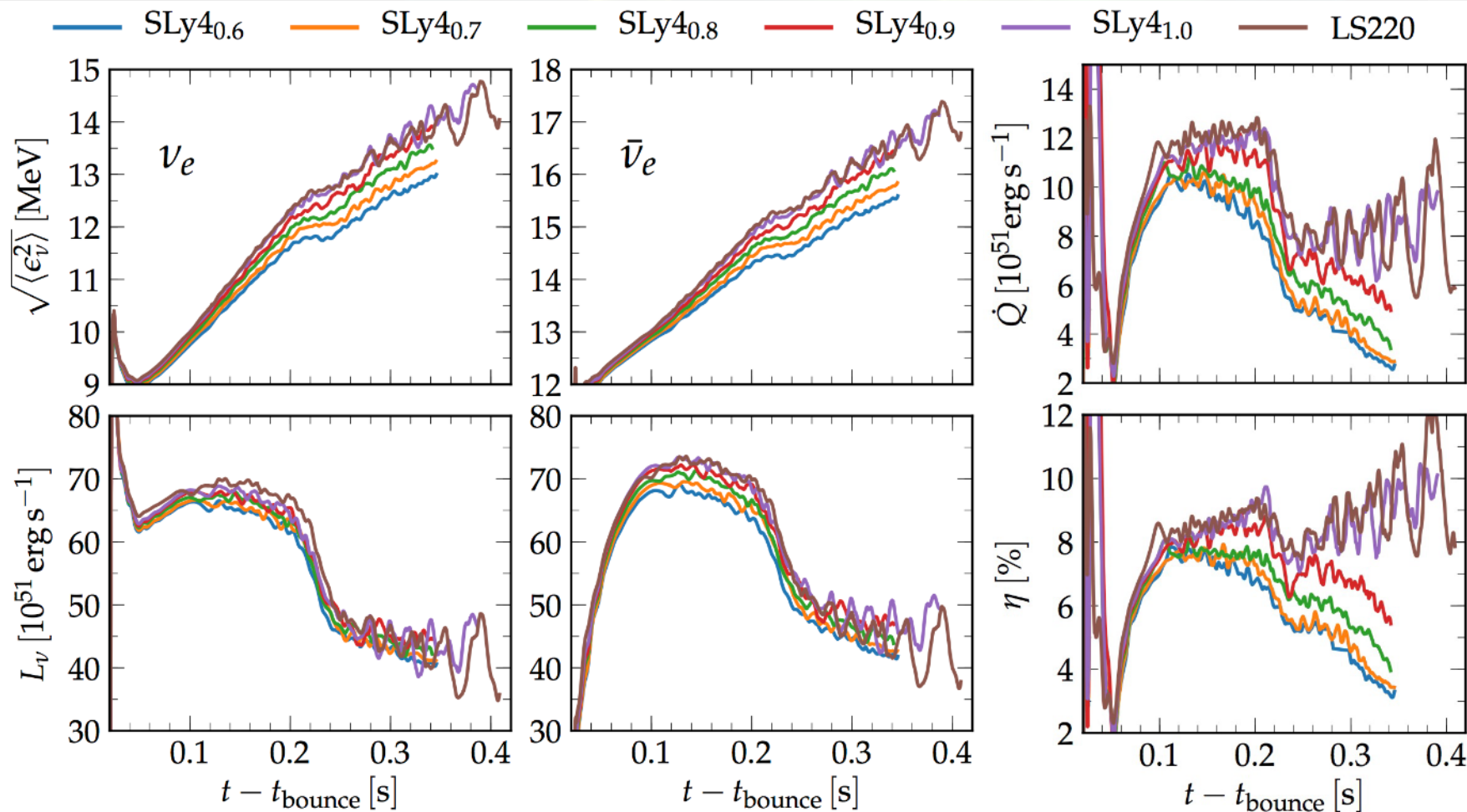
# It does impact the evolution in 3D!

da Silva Schneider et al.  
(2019b)

see also Yasin et al. (2018)



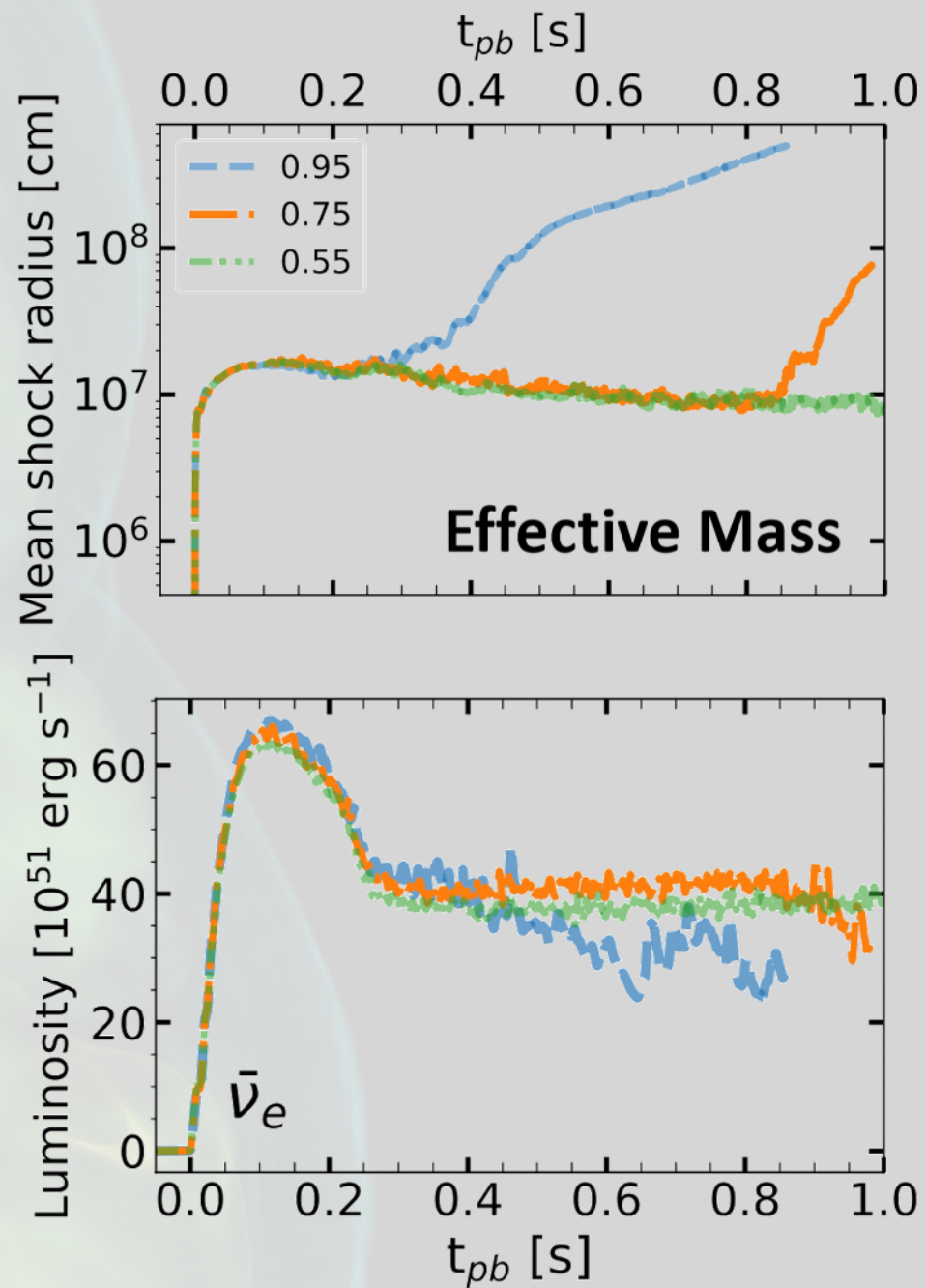
# high $m^*$ , less pressure, more compact, more heating



1. High effective mass gives lower thermal pressure,  $P_{\text{th}} \sim 1/m^*$
2. More compact protoneutron stars
3. More and hotter neutrinos
4. Greater heating and convection
5. Higher chance of explosion

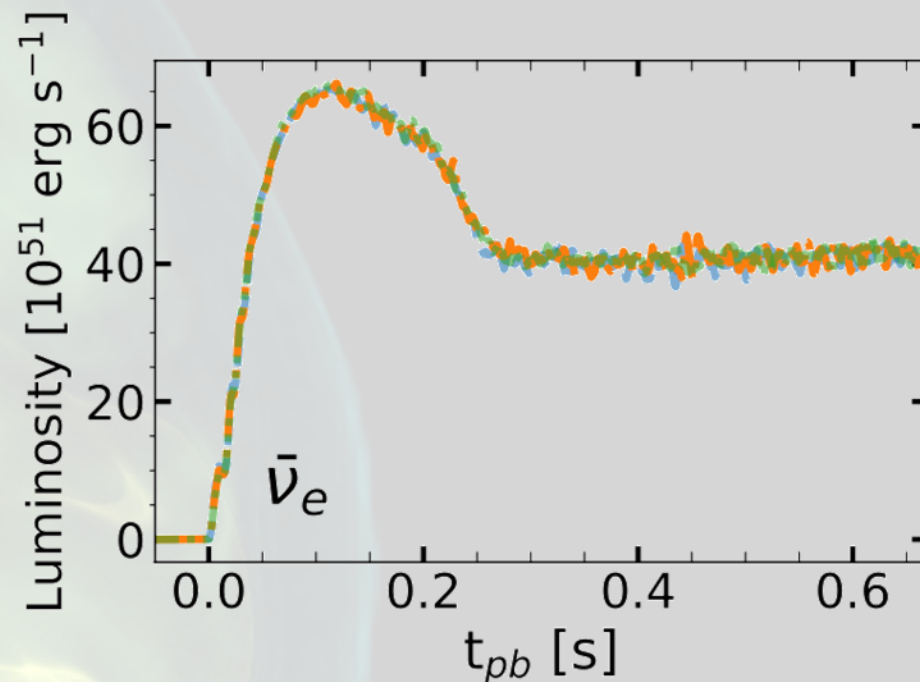
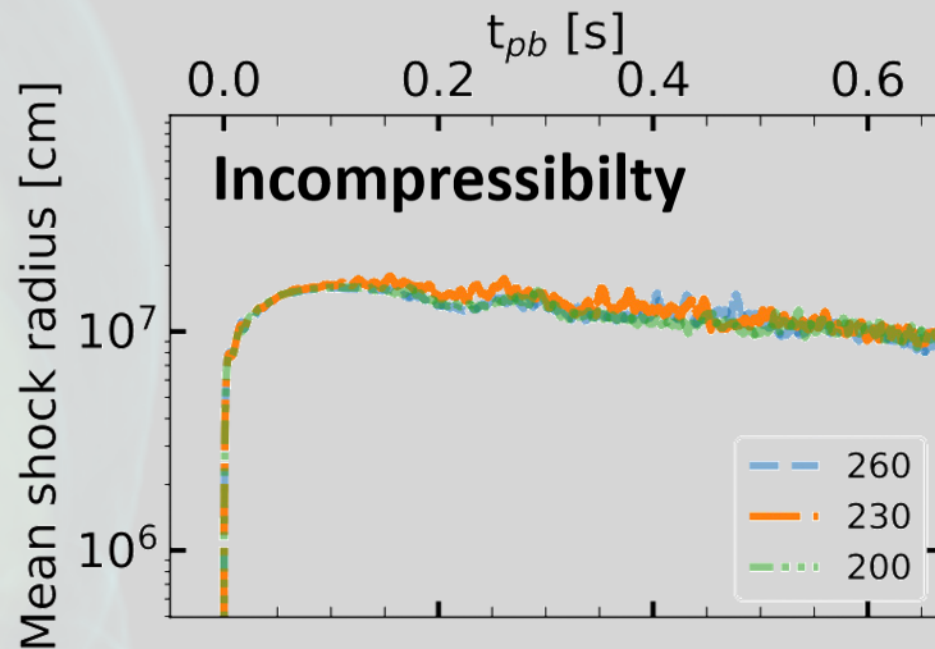
# Let's reenforce this idea

- Eggenberger Andersen et al. (2021)
  - 2D simulations
  - range of EOS with varying effective mass
  - Same result, low effective masses give more compact PNS, higher luminosities, energies, easier explosions



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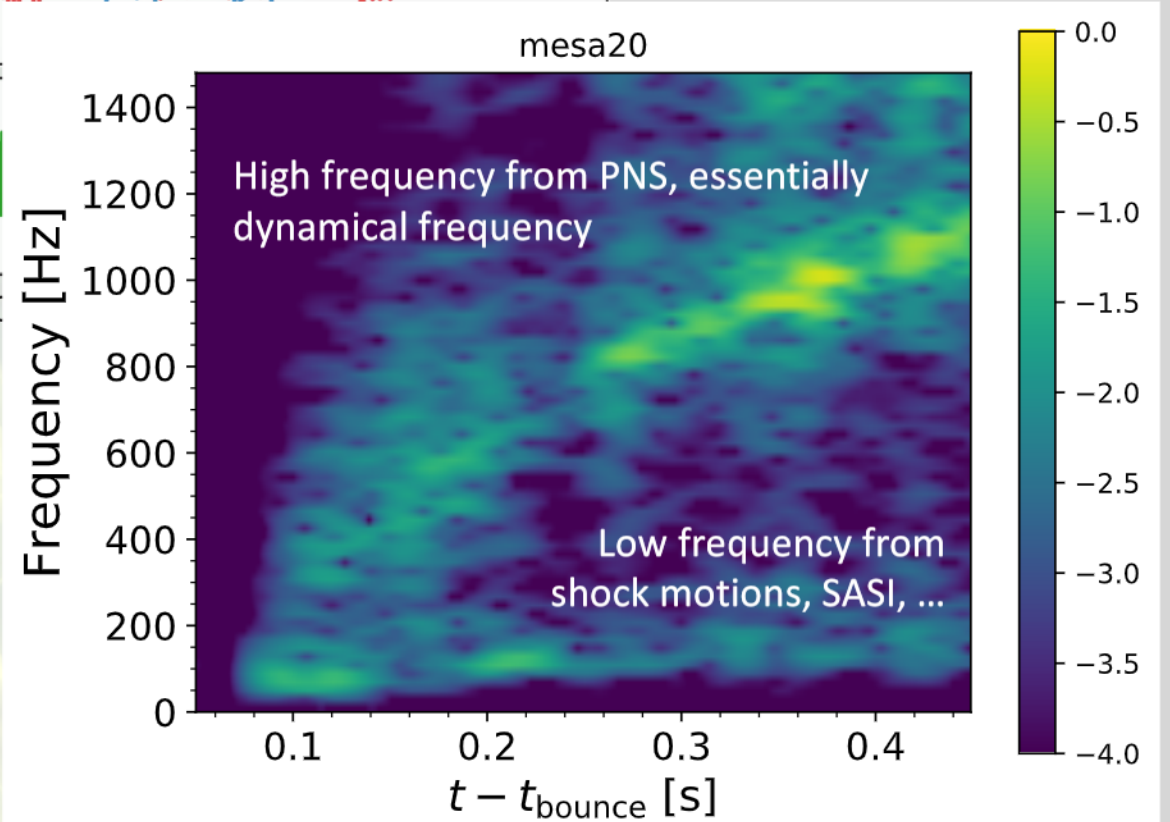
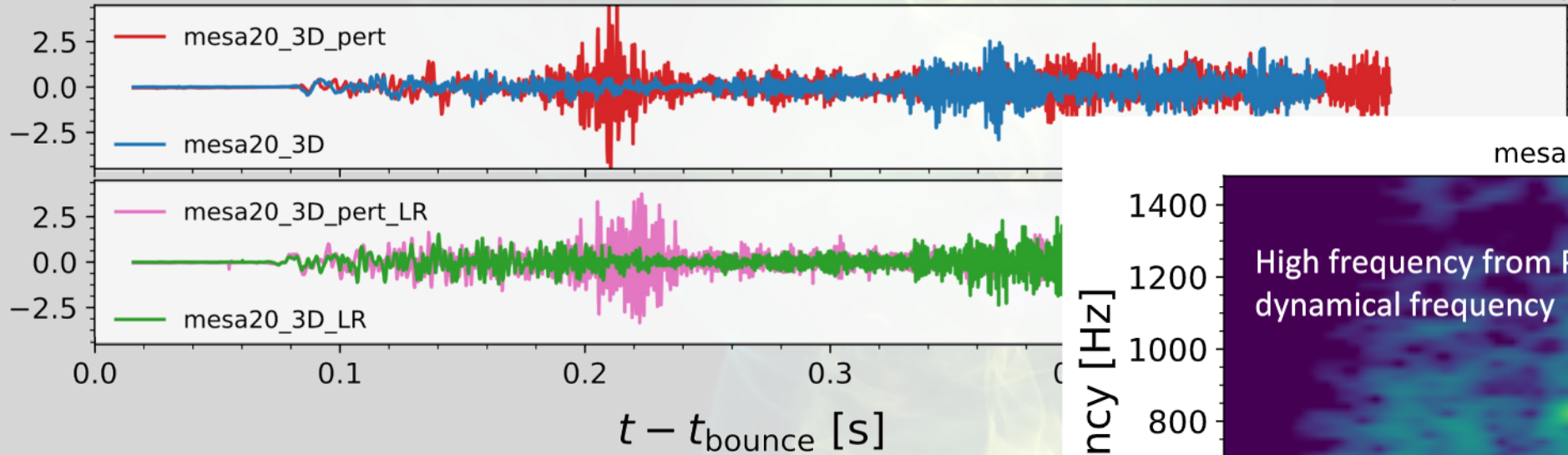
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  - range of EOS with varying effective mass
  - Same result, low effective masses give more compact PNS, higher luminosities, energies, easier explosions
- Variations in  $K_{\text{sat}}$  do not impact evolution nearly as much



# What other Multimessenger signals?

$$h_+^{\text{eq}} \times D \text{ [cm]}$$

EO & Couch (2018b)



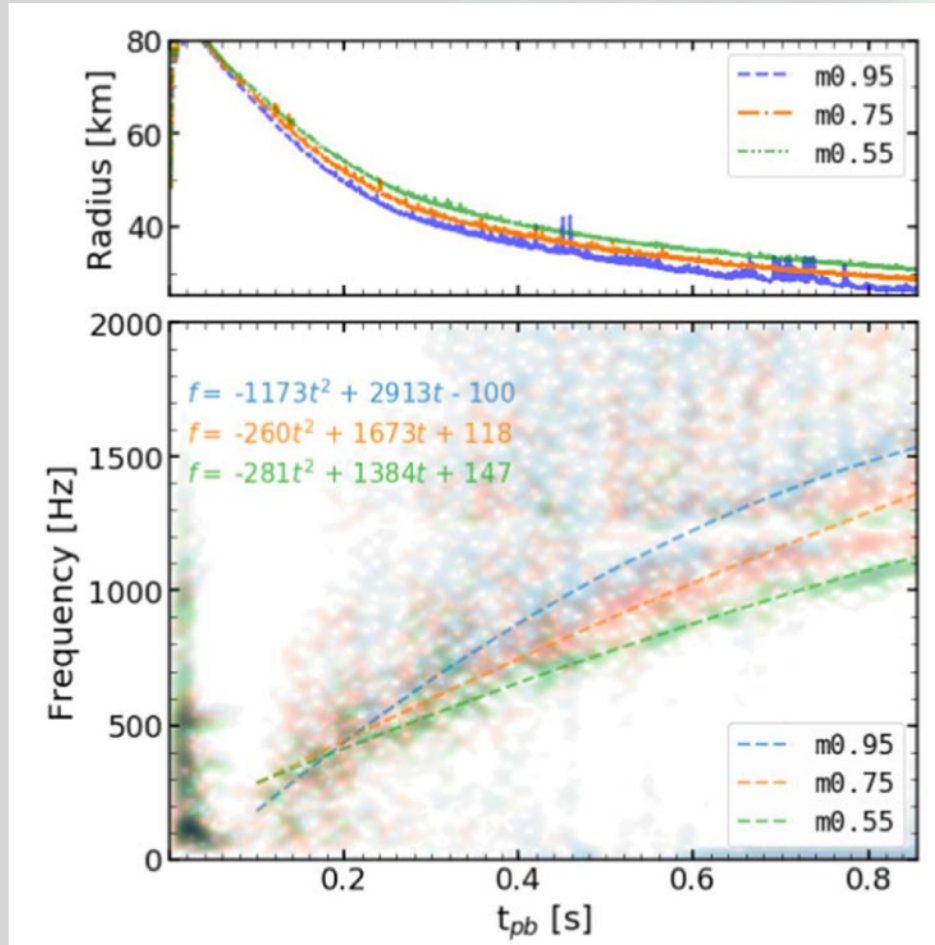
$$f_{\text{peak}} \approx \frac{1}{2\pi} \frac{GM}{R^2} \sqrt{1.1 \frac{m_n}{\langle E_{\bar{\nu}_e} \rangle} \left(1 - \frac{GM}{Rc^2}\right)^2}$$

Murphy et al. 2009, Marek et al. 2009, **Mueller et al. 2013**, ...

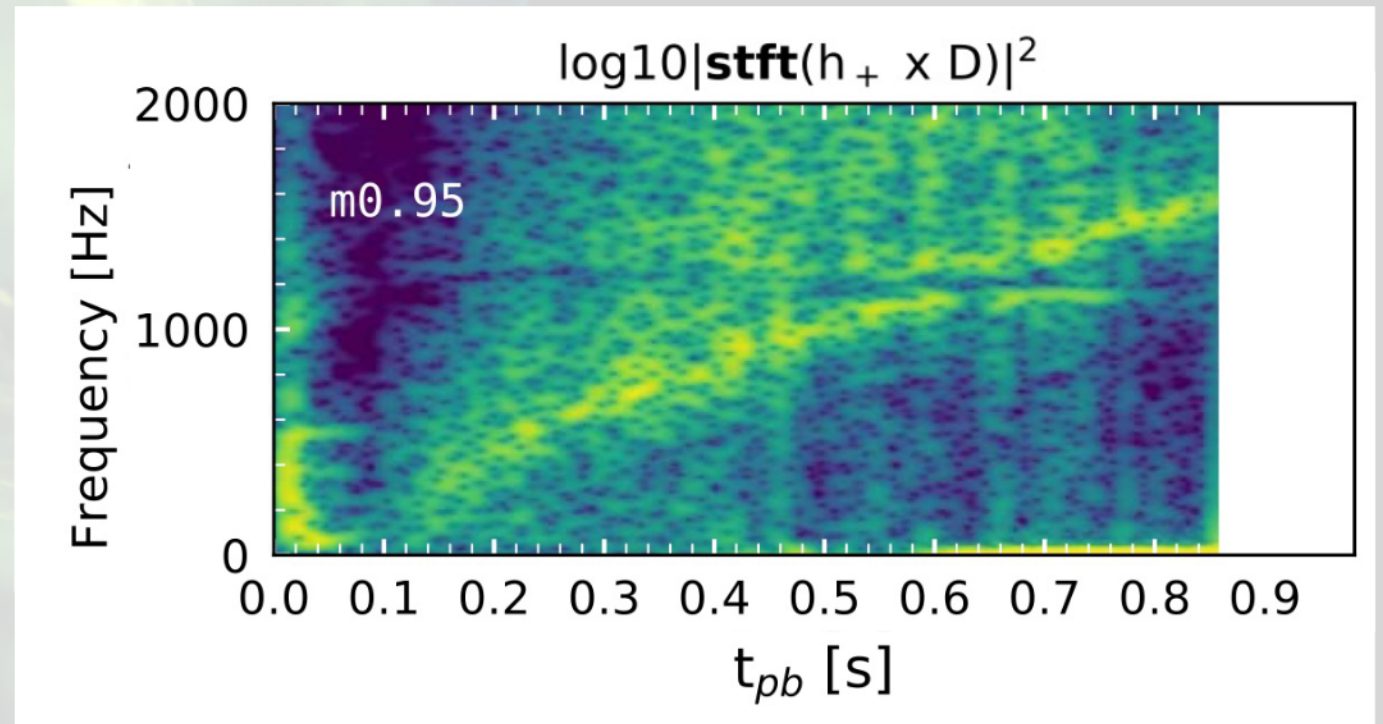


# Nuclear EOS and GWs

Eggenberger Andersen et al. (2021)



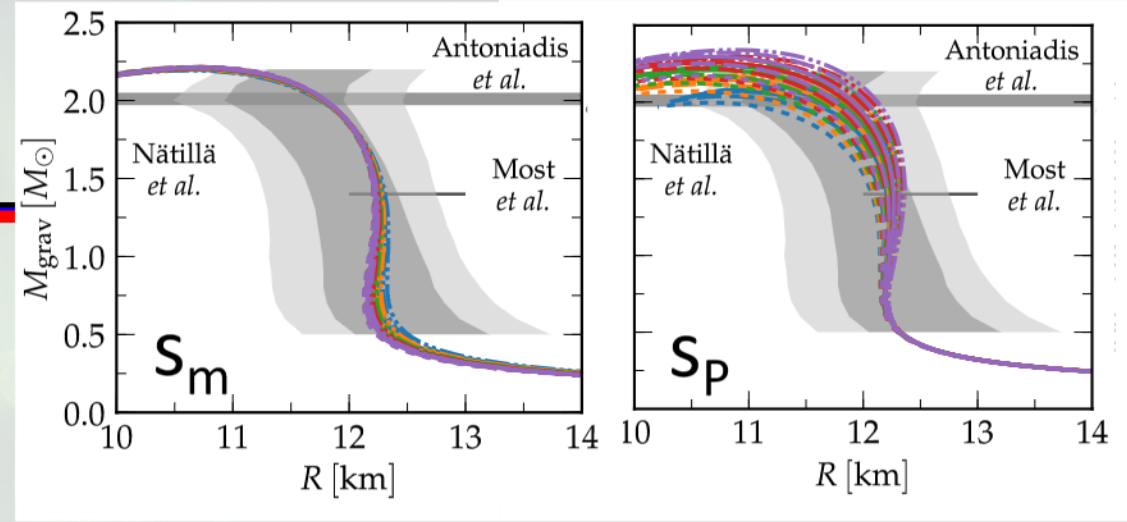
Eggenberger Andersen et al. (2021)



See also Fields et al. (2023) for impact in mergers!

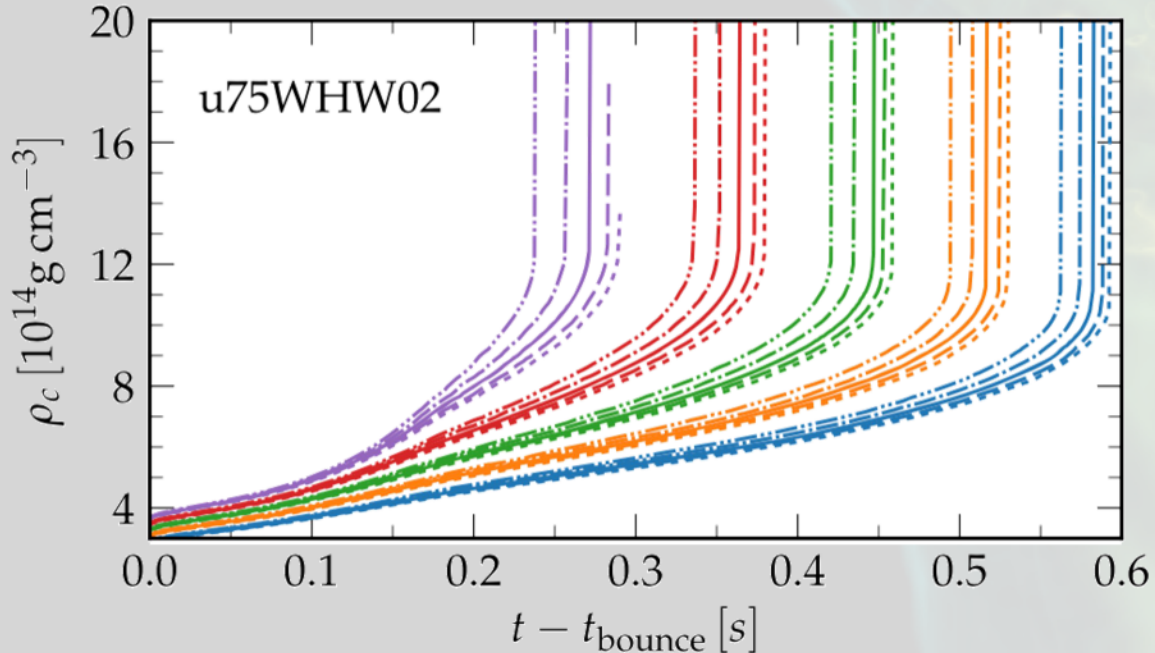
# Black Holes in 49 EOS

- What role do the thermal EOS and the cold EOS play in the black hole formation properties?

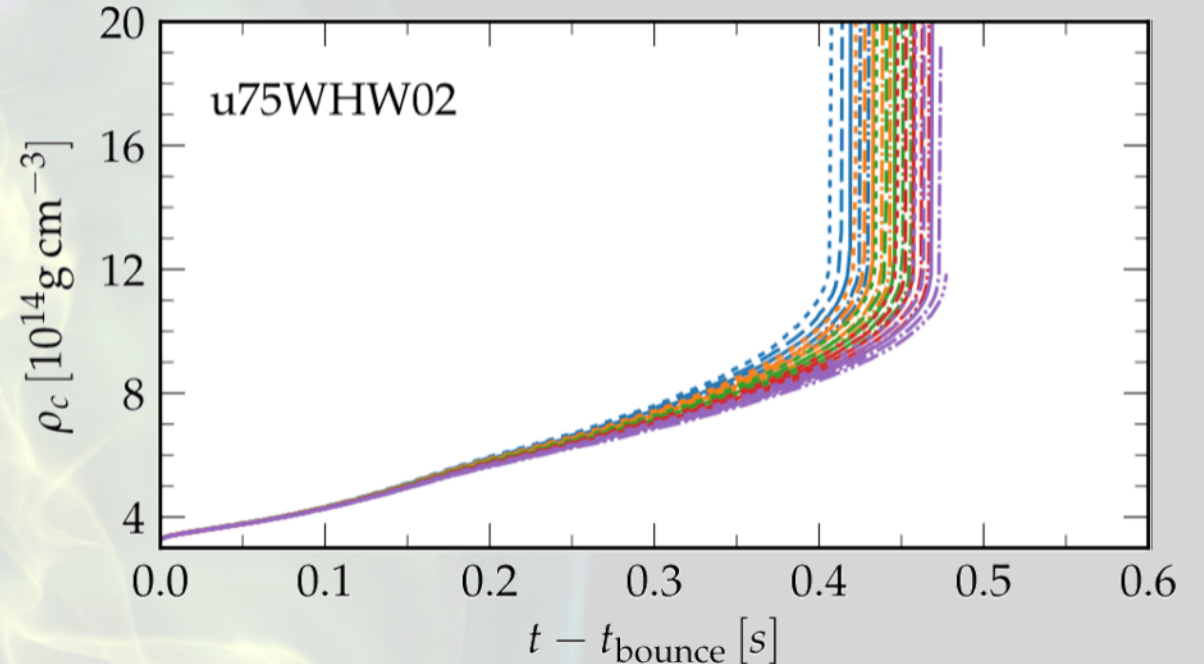


da Silva Schneider *et al.* (2020)

$m^* [m_n]$  : — 0.55 — 0.65 — 0.75 — 0.85 — 0.95  
 $\Delta m^* [m_n]$  : - - - -0.10 - - - 0.00 — 0.10 - - - 0.20 - - - 0.30

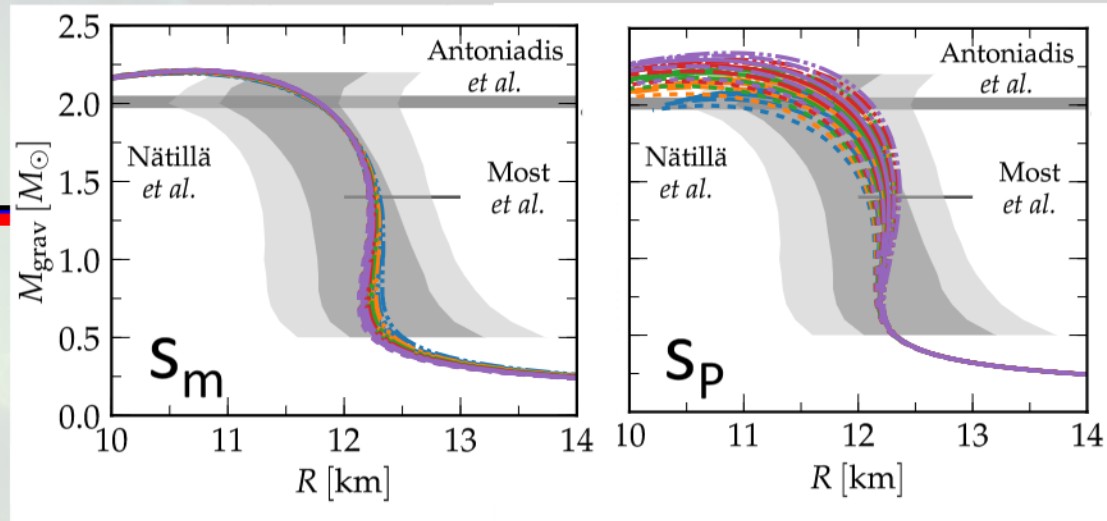


$P_{\text{SNM}}^{(4)} [\text{MeV fm}^{-3}]$  : — 100.0 — 112.5 — 125.0 — 137.5 — 150.0  
 $P_{\text{PNM}}^{(4)} [\text{MeV fm}^{-3}]$  : - - - 160.0 - - - 180.0 — 200.0 - - - 220.0 - - - 240.0

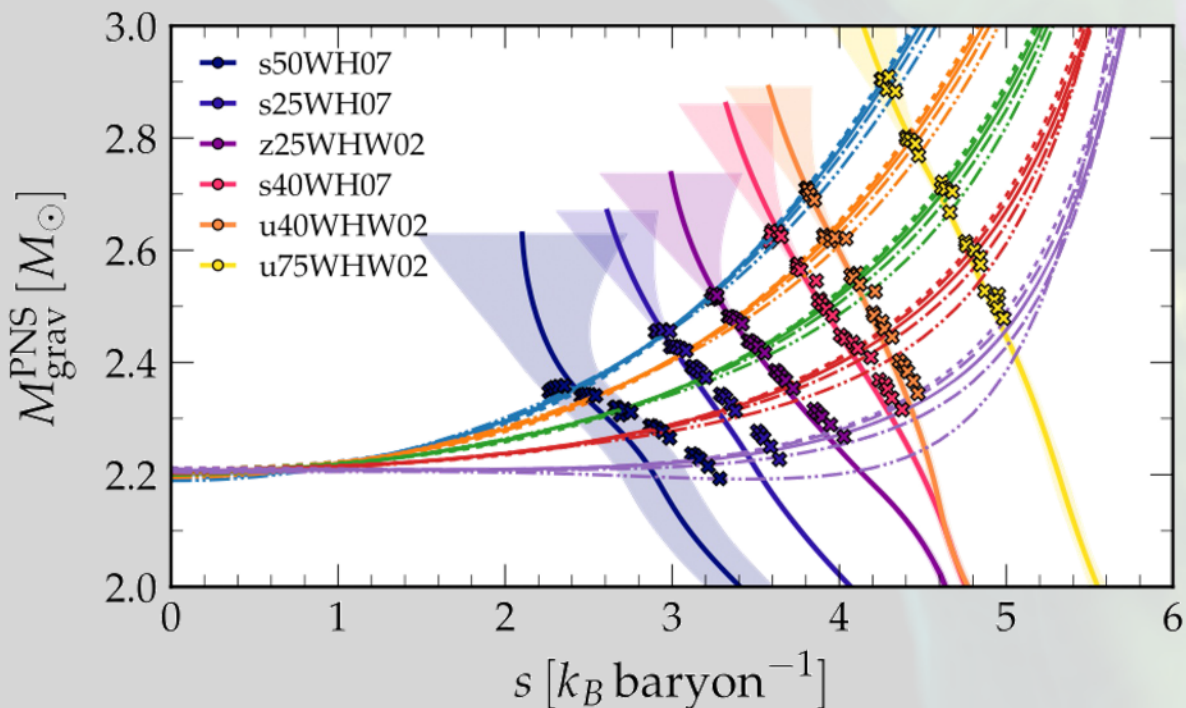


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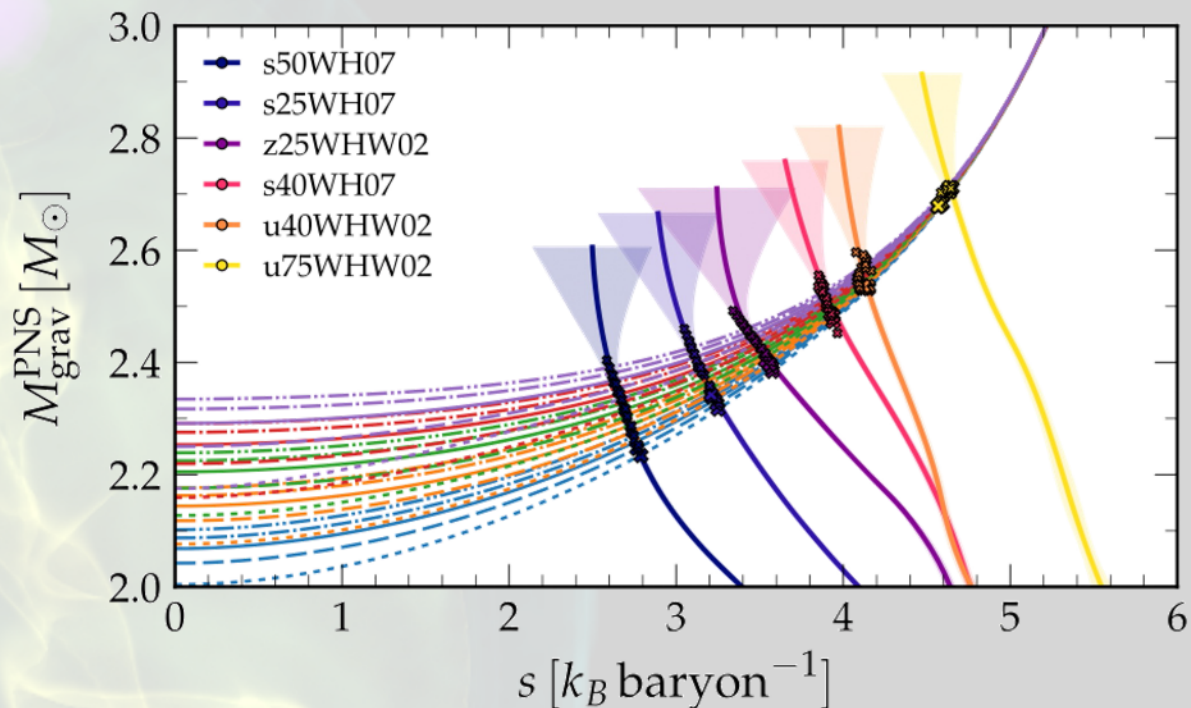
- Need to consider a hot PNS (we take constant entropy; see Hempel et al. 2013)



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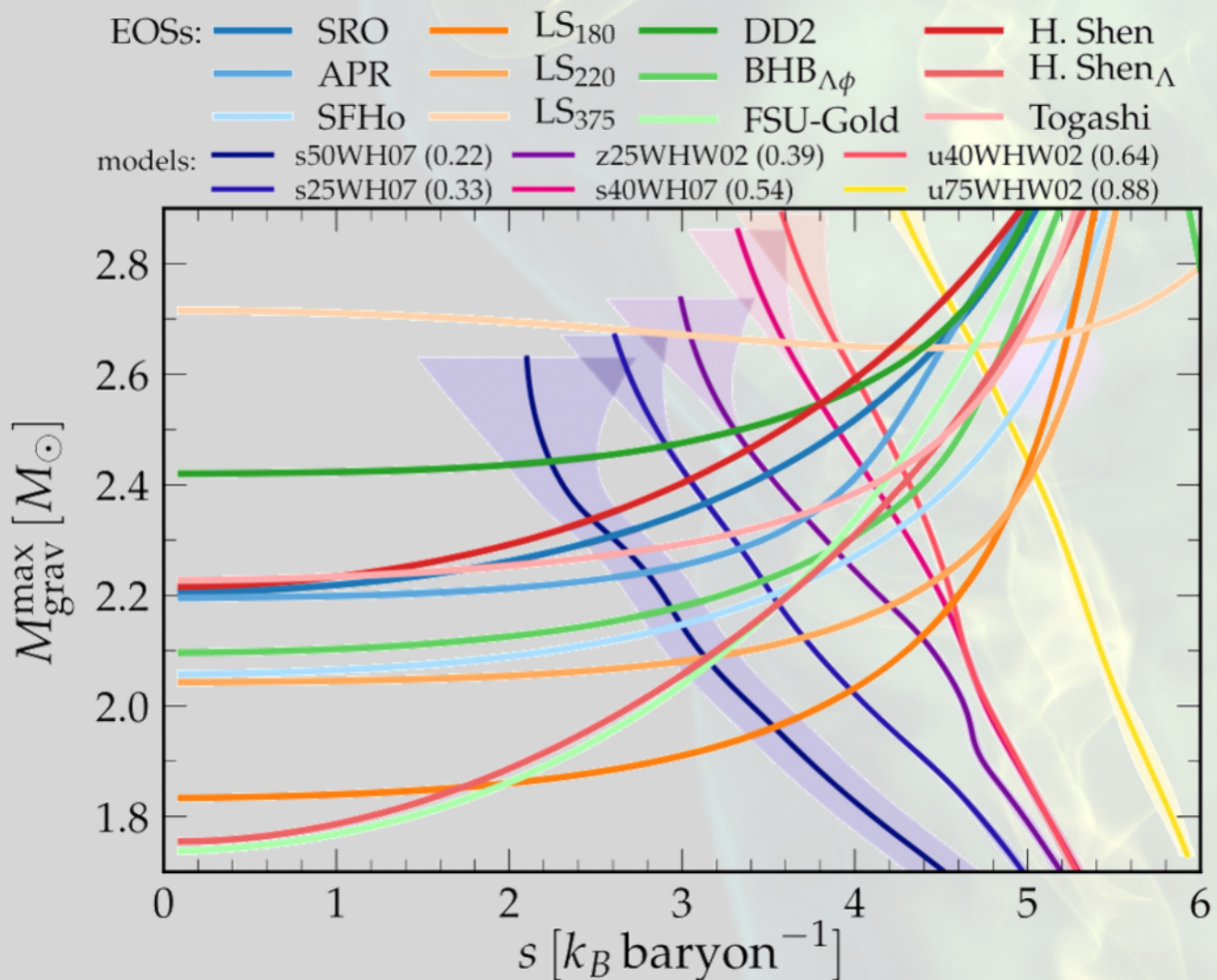


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# Thermal Landscape for Supernovae

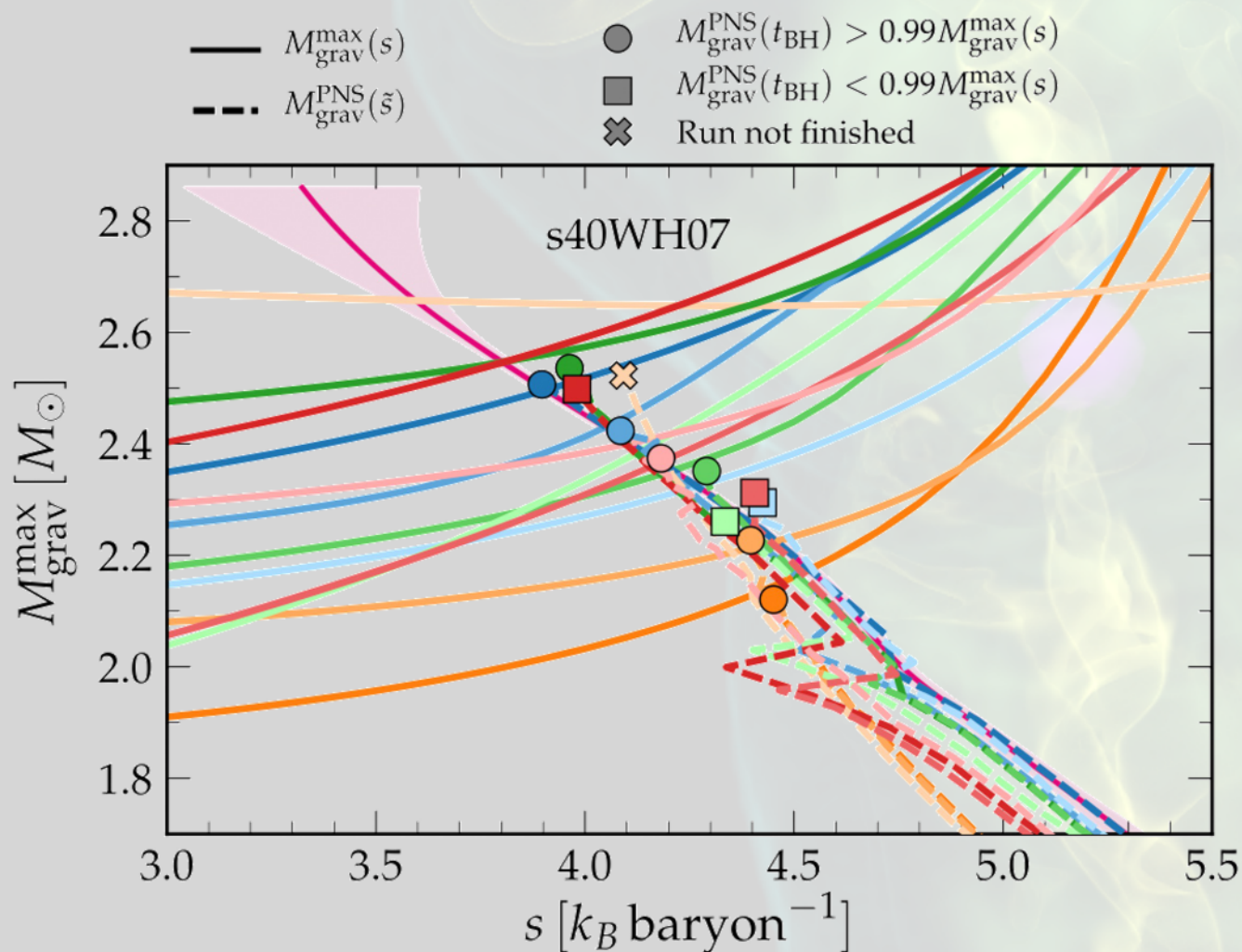
Schneider et al. (2020)



- A wider spread of finite temperature EOS have a much more rich variety of thermal effects
- Still follow the trend for black hole formation

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Schneider et al. (2020)

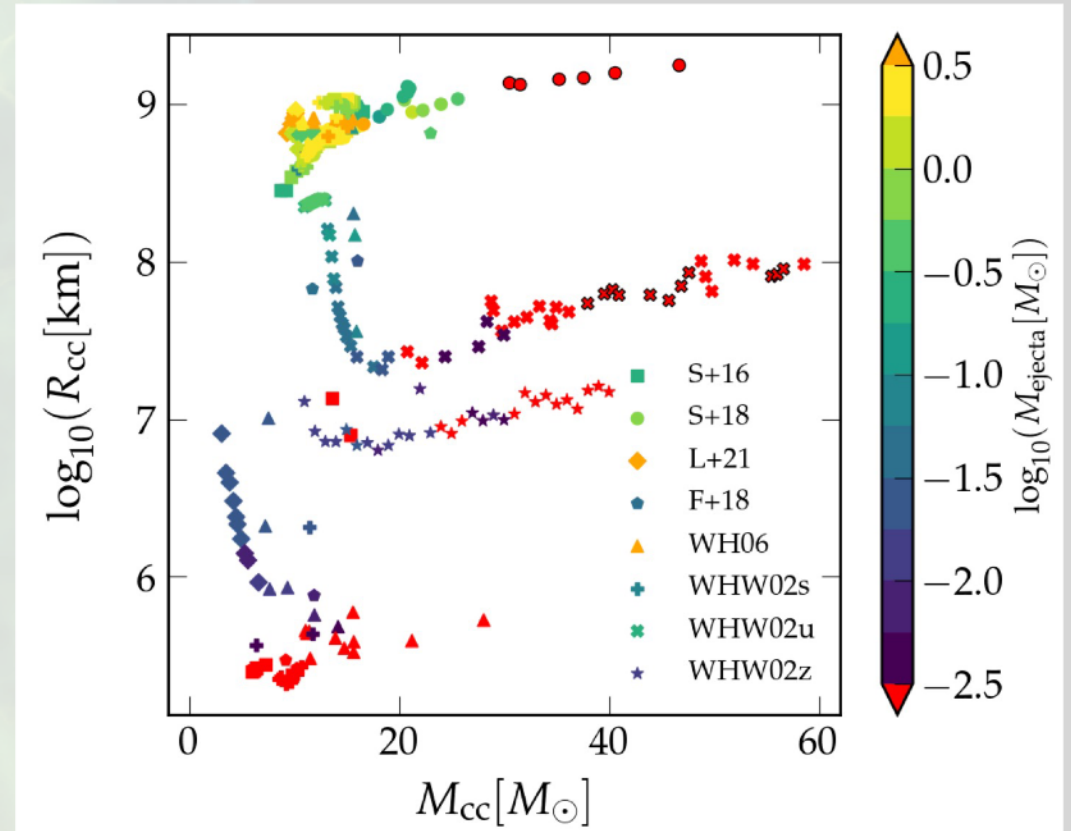


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# Impact on Ejecta in Failed Supernovae

- Not all core collapse events result in an explosion, some fraction of “Failed Supernovae”
- Such events can still eject mass due to neutrino emission (Nadyozhin 1980, Lovegrove & Woosley 2013, Fernandez et al. 2018, da Silva Schneider & EO 2022).

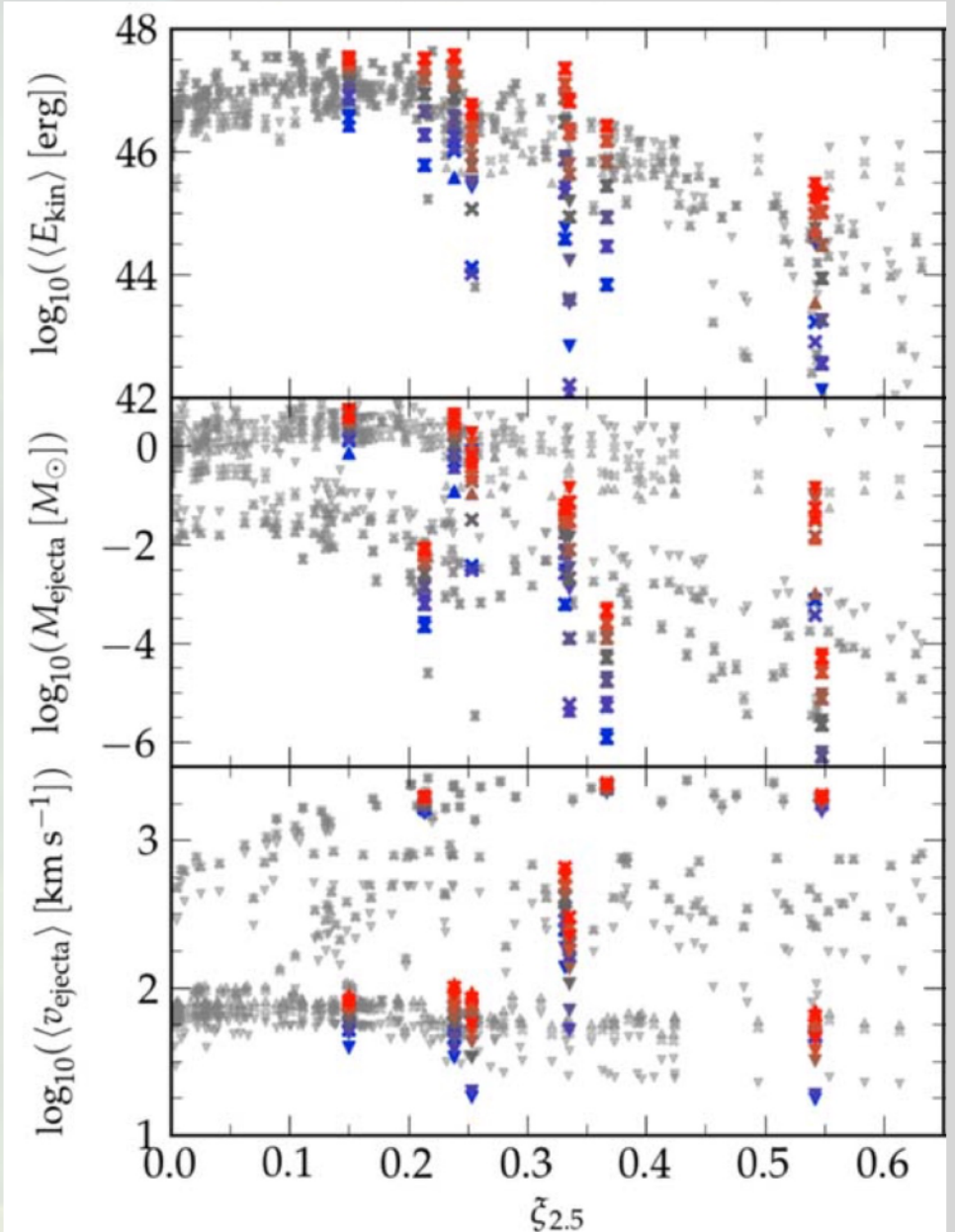
- Considerable energy carried away by neutrinos (several tenths of solar mass)
- Disrupts the hydrostatic balance throughout the star, pressure gradients dominates over gravity
- Sound pulse moves up, steepens to shock, can unbind loosely bound material



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# Summary

- The nuclear matter in supernovae (and merging neutron stars) is **hot** and behaves differently than cold nuclear matter
- One parameterization of this is through the effective mass, the thermal pressure is proportional  $1/m^*$
- low  $m^*$   $\rightarrow$  high thermal pressure  $\rightarrow$  puffed up PNS  $\rightarrow$  less, later, and less energetic explosions; lower frequency GWs; low  $m^*$   $\rightarrow$  high thermal pressure  $\rightarrow$  longer lifetimes  $\rightarrow$  delayed black hole formation
- Really hot PNS are quite insensitive to high density EOS, dominated by thermal response.